

# How does a GPS signal look ?

## MGA Webinar Series # 13

Dr. Dinesh Manandhar, Associate Professor (Project)  
Center for Spatial Information Science, The University of Tokyo

14<sup>th</sup> MAY 2020, 18:00 – 19:00 (JST)

ZOOM Link:

Registration: <https://gnss.peatix.com>

# Introduction

This webinar provides information on GPS L1C/A signal structure, signal generation and its properties like power spectrum, signal power. A software generated signal will be used for demonstration to show its properties like modulation, power spectrum and measurement of these power values using a Tektronix RSA 306B spectrum analyzer.

This webinar will help you to understand and visualize GPS signal. GPS L1C/A signal is a base signal for many other GNSS signals. If you are interested in signal processing, jamming, interference and spoofing (JIS) issues, then this webinar will provide necessary information required to understand JIS mitigation techniques. We will conduct webinar on JIS in near future.

DATE: 14th MAY 2020 (Thursday)

TIME: 18:00 - 19:00 JST (Japan Time)

Registration: <https://gpsca.peatix.com>

Main Link: <https://gnss.peatix.com> (Registration is required)



# GPS L1C/A Signal Structure

- Carrier Signal
  - It defines the frequency of the signal
  - For example:
    - GPS L1 is 1575.42MHz, L2 is 1227.60MHz and L5 is 1176.45MHz
- PRN (Pseudo Random Noise) Code
  - Randomly generated codes following a particular rule
  - Used to modulate the data and identify each satellite
  - Should have good auto-correlation and cross-correlation properties
- Navigation Data
  - Required to compute distance between the satellite and the receiver
  - Provides satellite orbit related data (ephemeris data)
  - Provides satellite clock related information (clock errors etc)
  - Provides satellite health related information to receiver

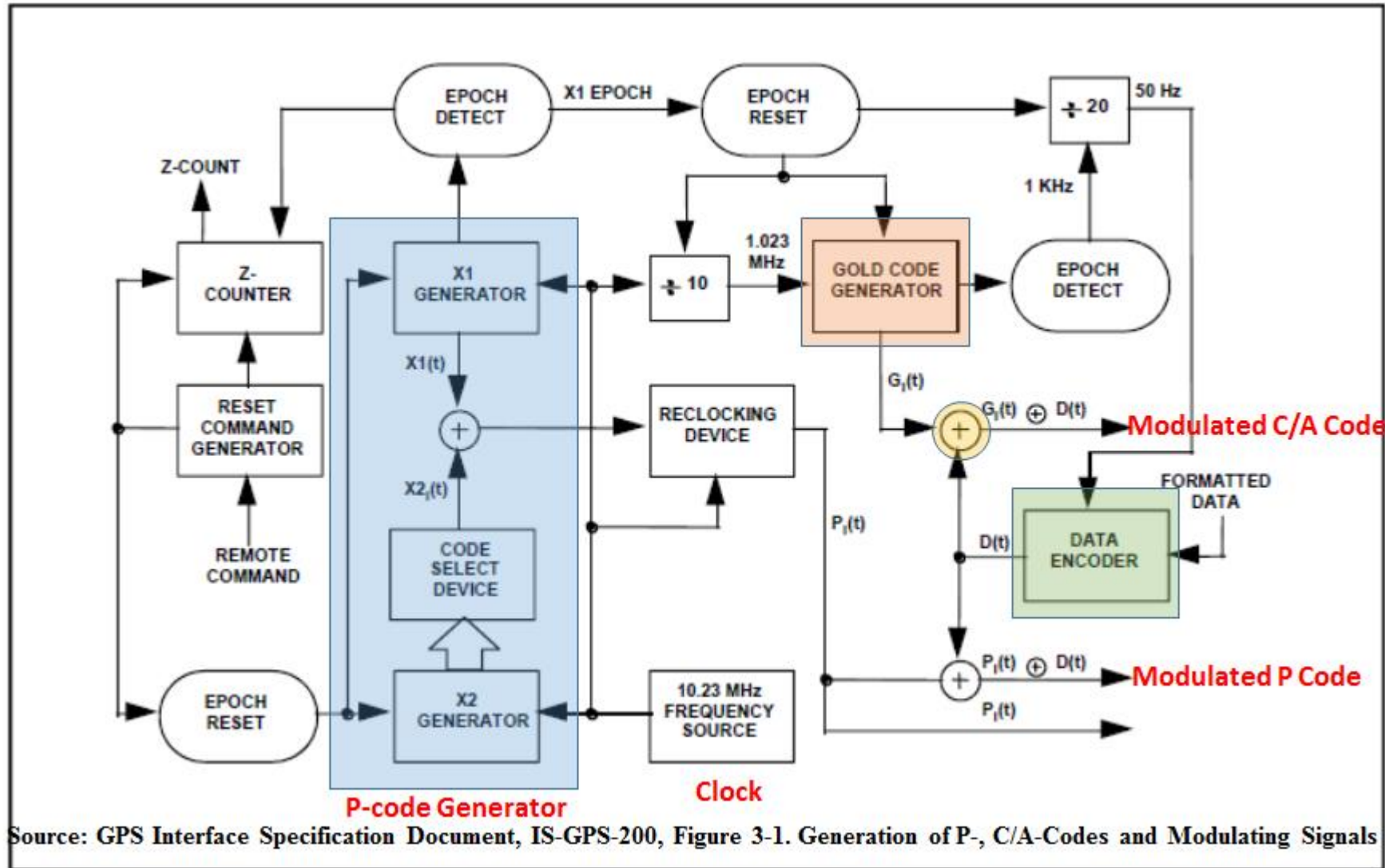
# GPS L1C/A Signal Structure

- Carrier Signal
  - Frequency : 1575.42MHz
- PRN Code
  - Chip Rate : 1.023MHz
  - Code Period : 1msec
  - No of Chips/Period : 1023
- Navigation Data
  - Data Rate : 50bps (bits per sec)
  - Bit Length : 20msec
- Modulation : BPSK(1)
  - BPSK (Binary Phase Shift Keying)

# GPS Signals

Band	Frequency, MHz	Signal Type	Code Length msec	Chip Rate, MHz	Modulation Type	Data / Symbol Rate, bps/sps	Notes
L1	1575.42 (10.23*154)	C/A	1	1.023	BPSK	50	Legacy Signal
		C <sub>Data</sub>	10	1.023	BOC(1,1)	50 / 100	
		C <sub>Pilot</sub>	10	1.023	TMBOC	No Data	BOC(1,1) & BOC(6,1)*
		P(Y)	7 days	10.23	BPSK		Restricted / Military
L2	1227.60 (10.23*120)	CM	20	0.5115	BPSK	25 / 50	Modulated by TDM of (L2CM xor Data) and L2CL
		CL	1500	0.5115		No Data	
		P(Y)	7days	10.23	BPSK		Restricted / Military
L5	1176.45 (10.23*115)	I	1	10.23	BPSK	50 / 100	Provides Higher Accuracy
		Q	1			No Data	

# GPS L1C/A, P Signals



IS-GPS-200H  
24-SEP-2013

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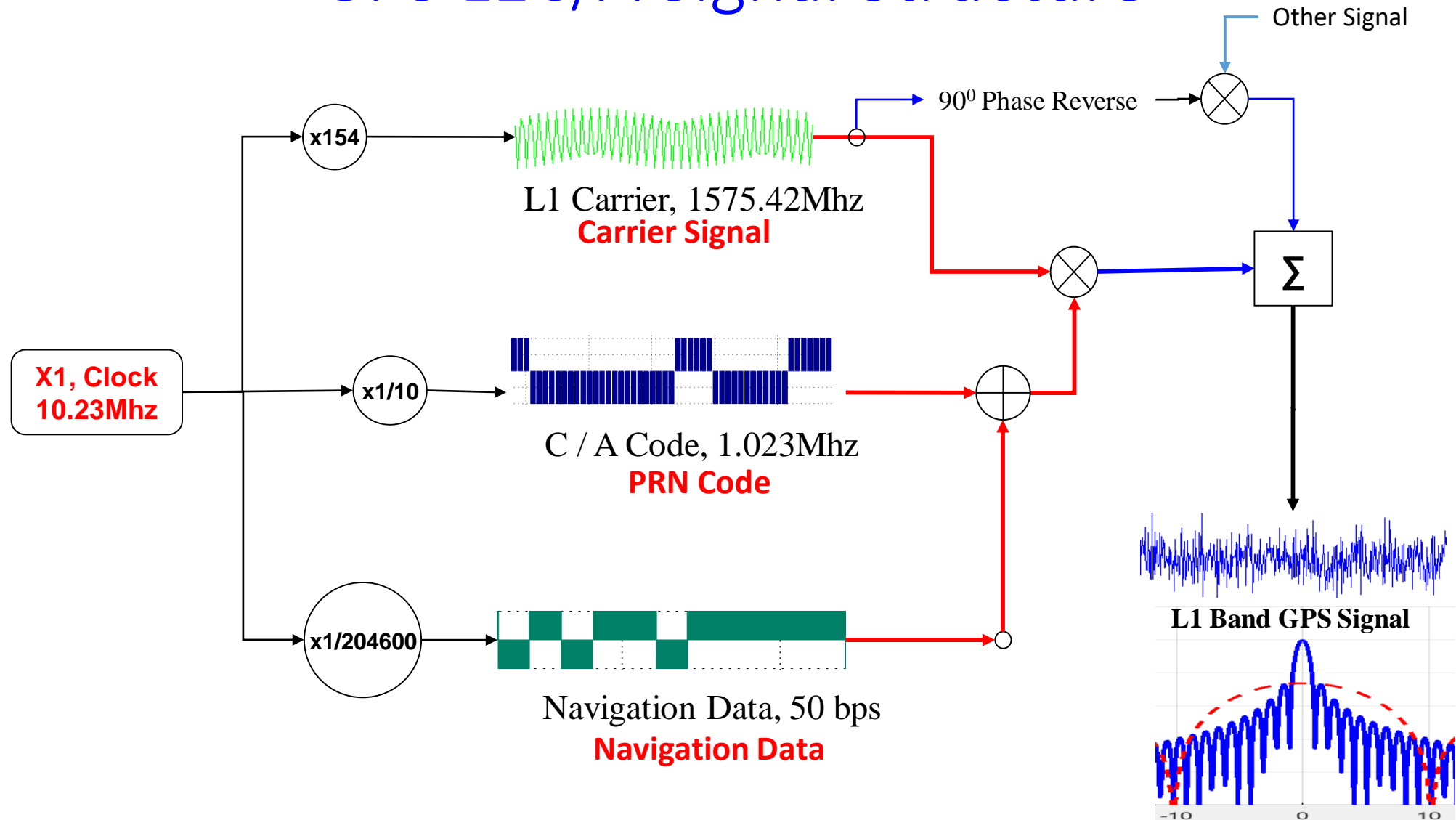
INTERFACE SPECIFICATION  
IS-GPS-200

Navstar GPS Space Segment/Navigation User Interfaces

AUTHENTICATED BY: *Michael J. Dunn* 21 MAR 14  
Michael J. Dunn, DISL, DAF  
Technical Director  
Global Positioning Systems Directorate

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# GPS L1C/A Signal Structure



# GPS L1 C/A PRN CODE

SV ID No.	GPS PRN Signal No.	Code Phase Selection		Code Delay Chips		First 10 Chips Octal* C/A	First 12 Chips Octal P
		C/A(G2)***	(X2)	C/A	P		
1	1	2 ⊕ 6	1	5	1	1440	4444
2	2	3 ⊕ 7	2	6	2	1620	4000
3	3	4 ⊕ 8	3	7	3	1710	4222
4	4	5 ⊕ 9	4	8	4	1744	4333
5	5	1 ⊕ 9	5	17	5	1133	4377
6	6	2 ⊕ 10	6	18	6	1455	4355
7	7	1 ⊕ 8	7	139	7	1131	4344
8	8	2 ⊕ 9	8	140	8	1454	4340
9	9	3 ⊕ 10	9	141	9	1626	4342
10	10	2 ⊕ 3	10	251	10	1504	4343
11	11	3 ⊕ 4	11	252	11	1642	—
12	12	5 ⊕ 6	12	254	12	1750	—
13	13	6 ⊕ 7	13	255	13	1764	—
14	14	7 ⊕ 8	14	256	14	1772	—
15	15	8 ⊕ 9	15	257	15	1775	—
16	16	9 ⊕ 10	16	258	16	1776	—
17	17	1 ⊕ 4	17	469	17	1156	—
18	18	2 ⊕ 5	18	470	18	1467	—
19	19	3 ⊕ 6	19	471	19	1633	4343

\* In the octal notation for the first 10 chips of the C/A code as shown in this column, the first digit (1) represents a "1" for the first chip and the last three digits are the conventional octal representation of the remaining 9 chips. (For example, the first 10 chips of the C/A code for PRN Signal Assembly No. 1 are: 1100100000).

\*\* C/A Codes for 34 and 37 are identical.

\*\*\* The two-tap coder utilized here is only an example implementation that generates a limited set of valid C/A codes.  
⊕ = "exclusive or"

NOTE #1: The code phase assignments constitute inseparable pairs, each consisting of a specific C/A and a specific P code phase, as shown above.

SV ID No.	GPS PRN Signal No.	Code Phase Selection		Code Delay Chips		First 10 Chips Octal* C/A	First 12 Chips Octal P
		C/A(G2)****	(X2)	C/A	P		
20	20	4 ⊕ 7	20	472	20	1715	4343
21	21	5 ⊕ 8	21	473	21	1746	—
22	22	6 ⊕ 9	22	474	22	1763	—
23	23	1 ⊕ 3	23	509	23	1063	—
24	24	4 ⊕ 6	24	512	24	1706	—
25	25	5 ⊕ 7	25	513	25	1743	—
26	26	6 ⊕ 8	26	514	26	1761	—
27	27	7 ⊕ 9	27	515	27	1770	—
28	28	8 ⊕ 10	28	516	28	1774	—
29	29	1 ⊕ 6	29	859	29	1127	—
30	30	2 ⊕ 7	30	860	30	1453	—
31	31	3 ⊕ 8	31	861	31	1625	—
32	32	4 ⊕ 9	32	862	32	1712	—
65	33***	5 ⊕ 10	33	863	33	1745	—
66	34**	4 ⊕ 10	34	950	34	1713	—
67	35	1 ⊕ 7	35	947	35	1134	—
68	36	2 ⊕ 8	36	948	36	1456	—
69	37**	4 ⊕ 10	37	950	37	1713	4343

\* In the octal notation for the first 10 chips of the C/A code as shown in this column, the first digit (1) represents a "1" for the first chip and the last three digits are the conventional octal representation of the remaining 9 chips. (For example, the first 10 chips of the C/A code for PRN Signal Assembly No. 1 are: 1100100000).

\*\* C/A codes 34 and 37 are identical.

\*\*\* PRN sequence 33 is reserved for other uses (e.g. ground transmitters).

\*\*\*\* The two-tap coder utilized here is only an example implementation that generates a limited set of valid C/A codes.  
⊕ = "exclusive or"

NOTE #1: The code phase assignments constitute inseparable pairs, each consisting of a specific C/A and a specific P code phase, as shown above.

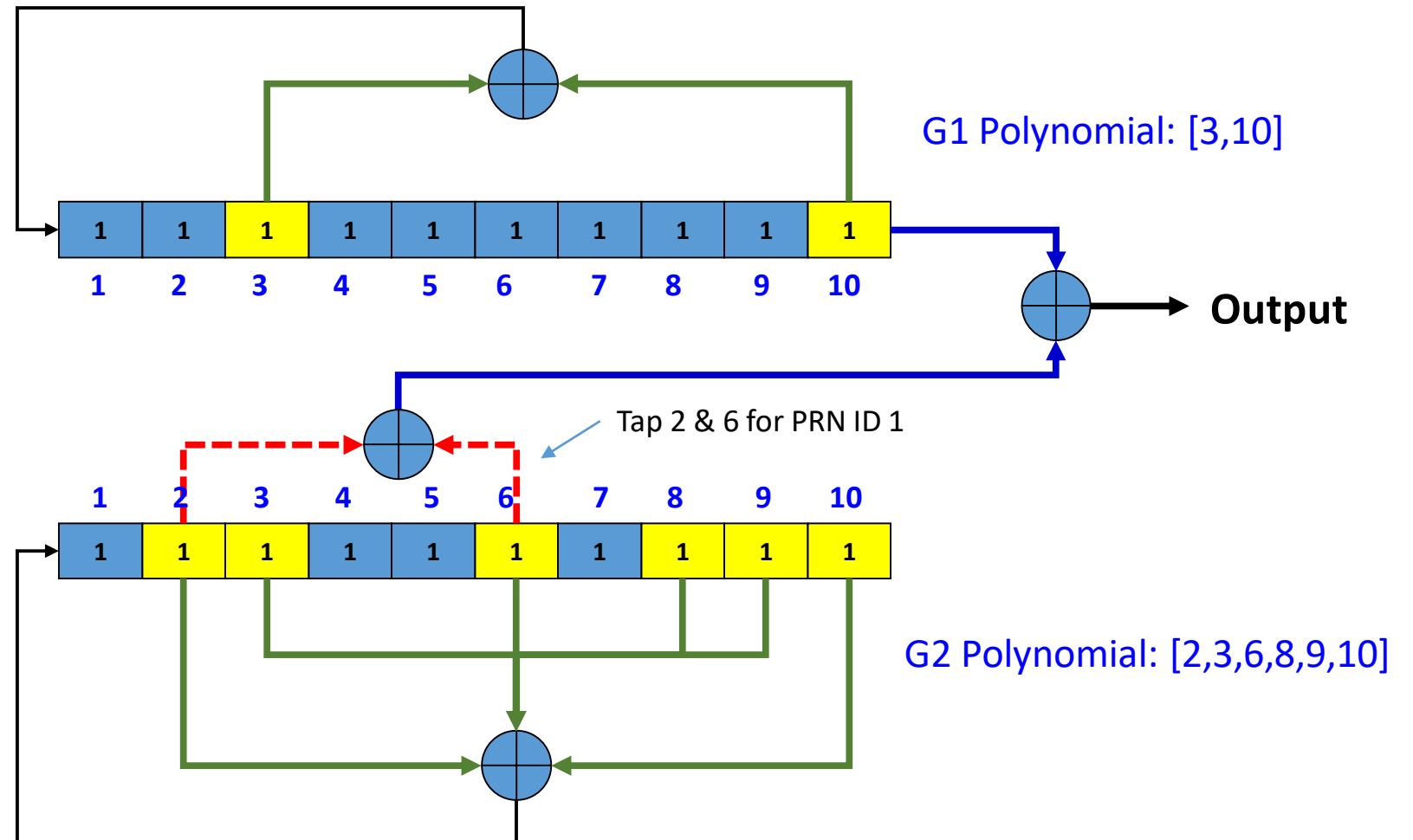
Source: GPS Interface Specification Document, IS-GPS-200,

Contact: dinesh@csis.u-tokyo.ac.jp, Center for Spatial Information Science, The University of Tokyo

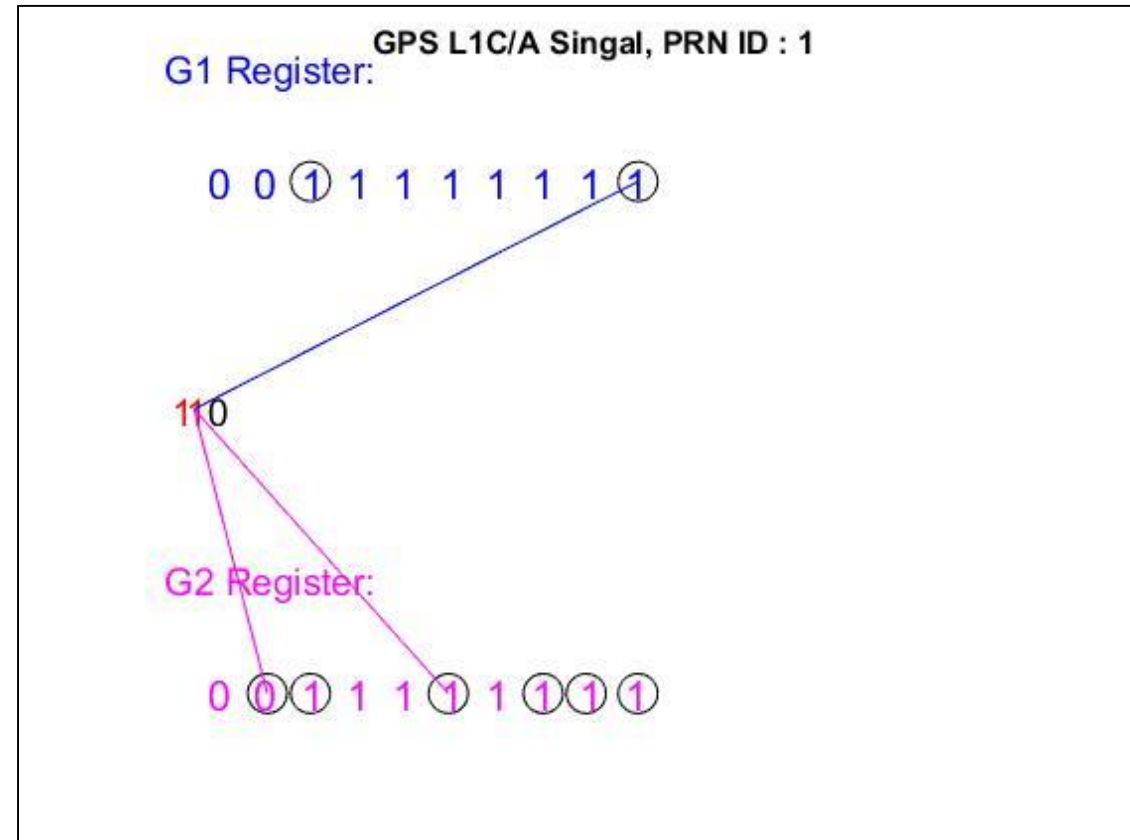
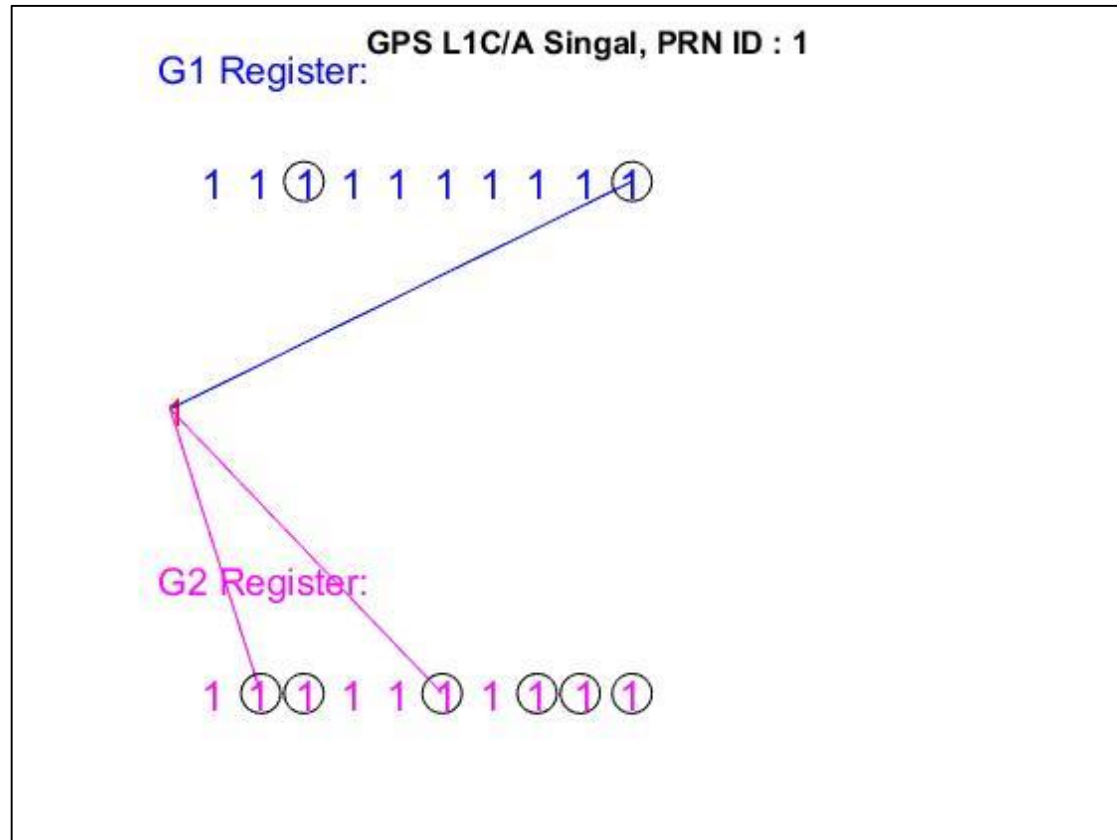


# Generation of GPS L1C/A PRN Code

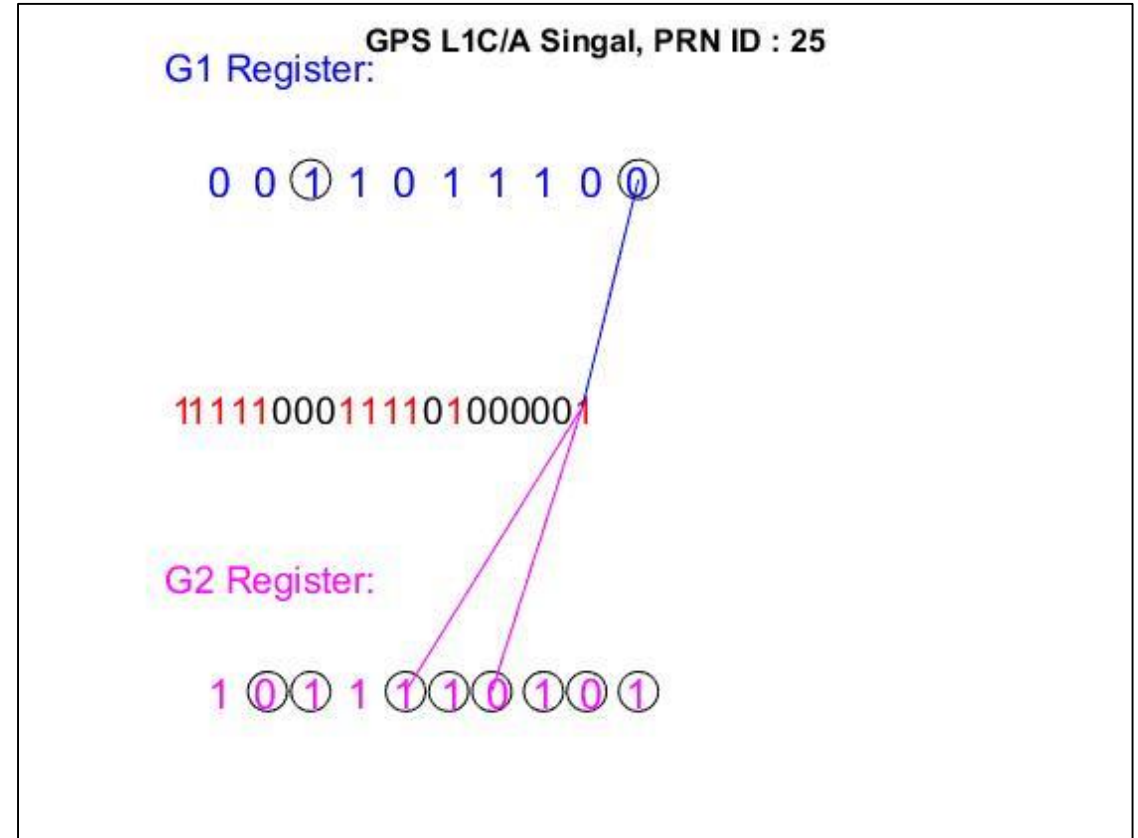
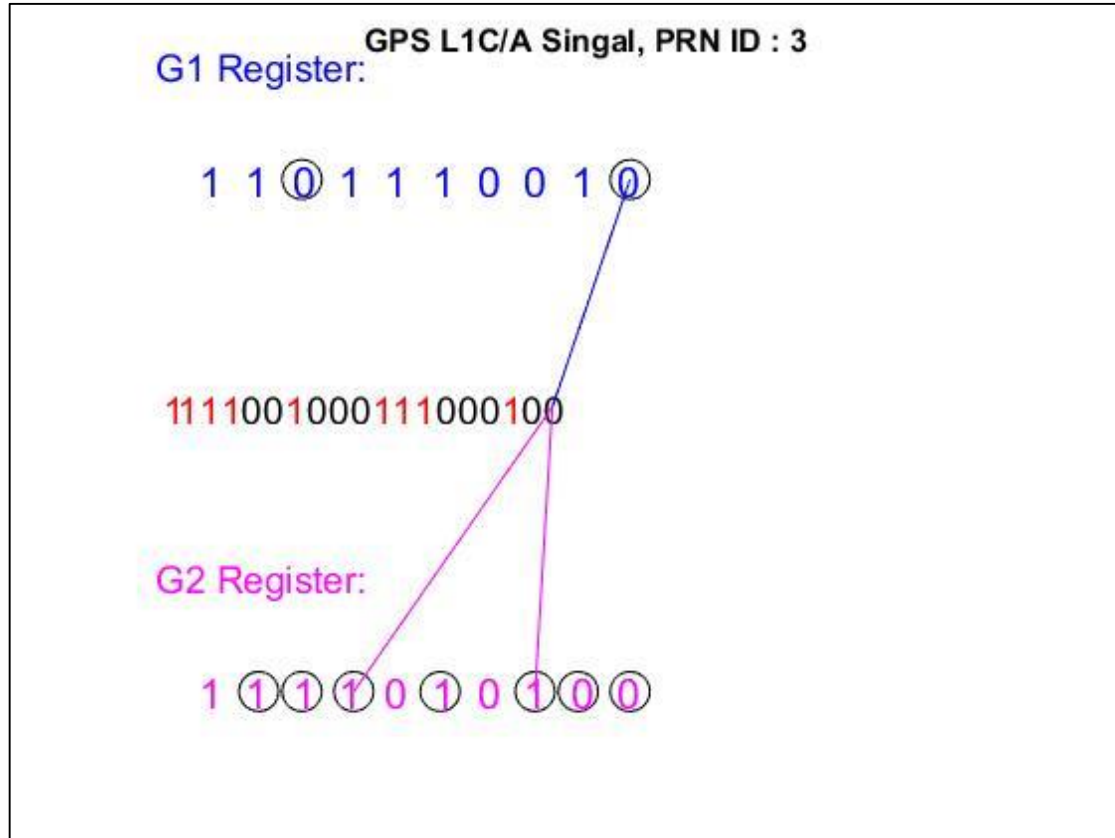
- Based on Gold Codes
- Use two 10 bit registers, G1 and G2 LFSR (Linear Feed Shift Register)
- All initial bits of registers are set at 1
- Taps 3 and 10 are used for G1
- Taps 2,3,6,8,9,10 are used for G2
- Two additional taps are selected based on PRN ID. See GPS IS document for the list of the taps.
- Example, Taps 2 and 7 are used for PRN ID 1.



# PRN Code Output #1



# PRN Code Output #3 and #25



# Modulo – 2 Operation

Represent all signals by “+1” or “-1” and use multiplication for Software Approach

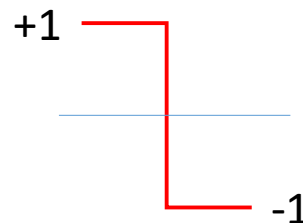
0	⊕	0	=	0
0	⊕	1	=	1
1	⊕	0	=	1
1	⊕	1	=	0

1	X	1	=	1
1	X	-1	=	-1
-1	X	1	=	-1
-1	X	-1	=	1

- Either use “0” and “1” or “1” and “-1”
- We need the code representation in “1” and “-1” format

Example:

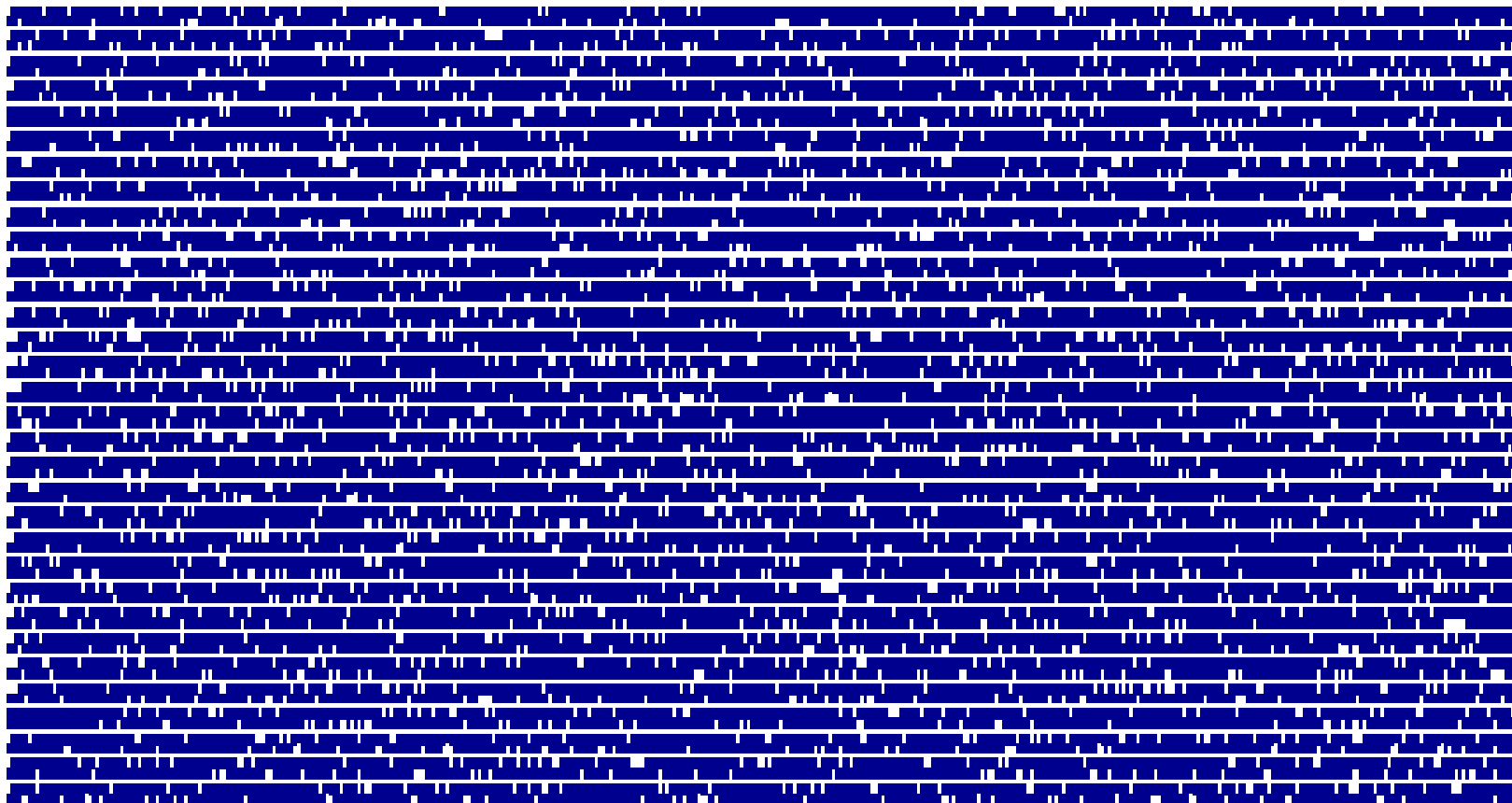
PRN 1 : 1 1 0 0 1 0 0 0 0..... Shall be  
-1 -1 1 1 -1 1 1 1 1 1 .....



- Represent “0” by “1” and “1” by “-1”
- Then multiply for Modulo - 2 operation
  - Simpler for programming
- Digital signal can have only “+1” or “-1”
- “1” or “0” means “ON” and “OFF”

# GPS L1 C/A Code of PRN 1 to 32

PRN 1- [  
PRN 2- [



C/A Codes for  
the First 10bits

PRN 1 : 1100100000

PRN 29 : 1001010111

PRN 32 : 1111001010

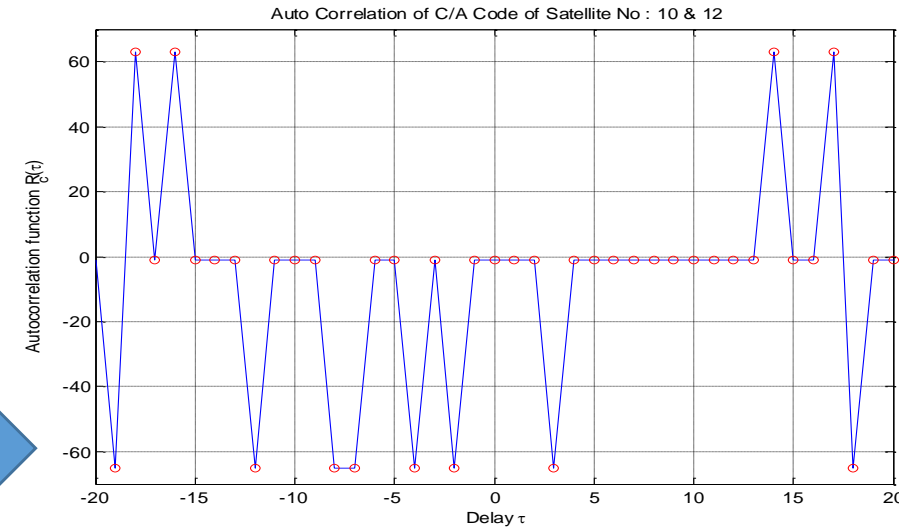
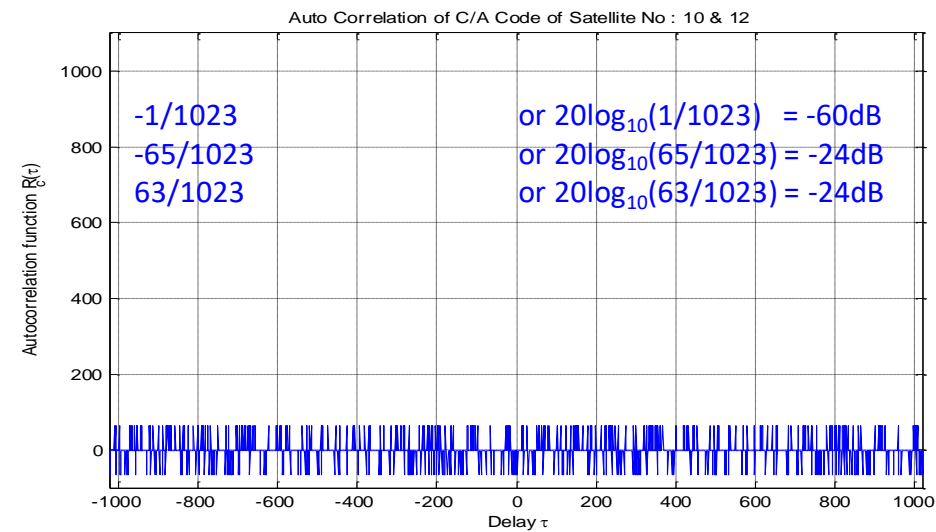
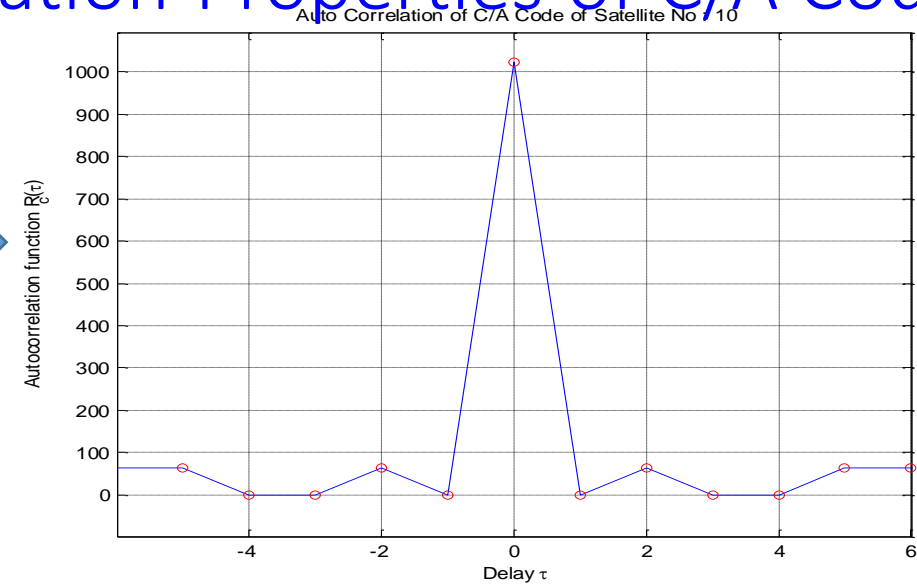
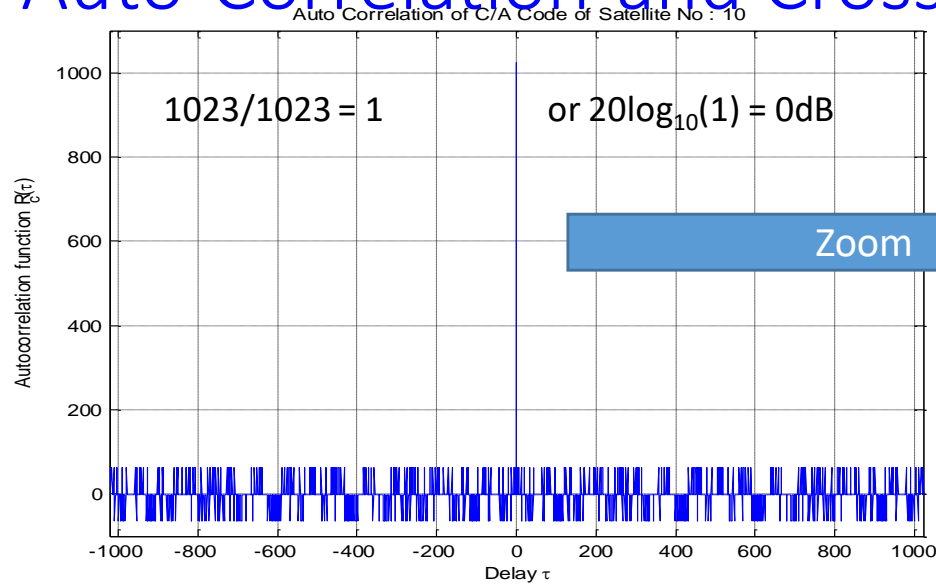
PRN 32- [

# Auto Correlation Property

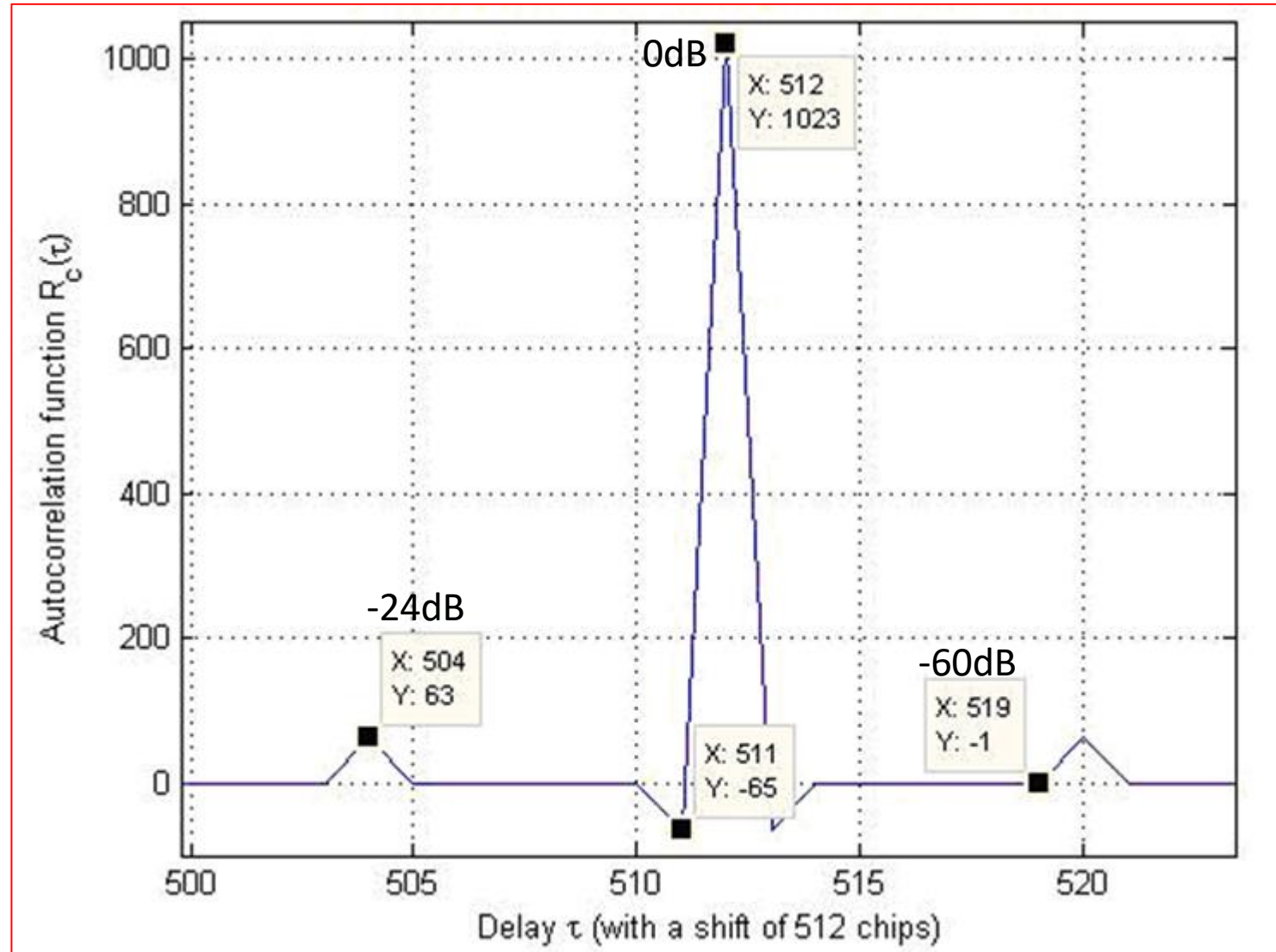
- Auto correlation Property of Gold Code when the shift is an integer multiple of a chip width is :
  - 1
  - $-1/N$
  - $-B(n)/N$
  - $[B(n)-2]/N$
  - Where  $B(n) = 1+2^{(n+2)/2}$ 
    - $n = 10$  for Gold Code that generates C/A code
  - Example :
    - $N = 2^n - 1 = 1023$  for  $n = 10$
    - Auto Correlation Values are
 

• $1023/1023 = 1$	or $20\log_{10}(1) = 0\text{dB}$
• $-1/1023$	or $20\log_{10}(1/1023) = -60\text{dB}$
• $-65/1023$	or $20\log_{10}(65/1023) = -24\text{dB}$
• $63/1023$	or $20\log_{10}(63/1023) = -24\text{dB}$

# Auto-Correlation and Cross-Correlation Properties of C/A Code



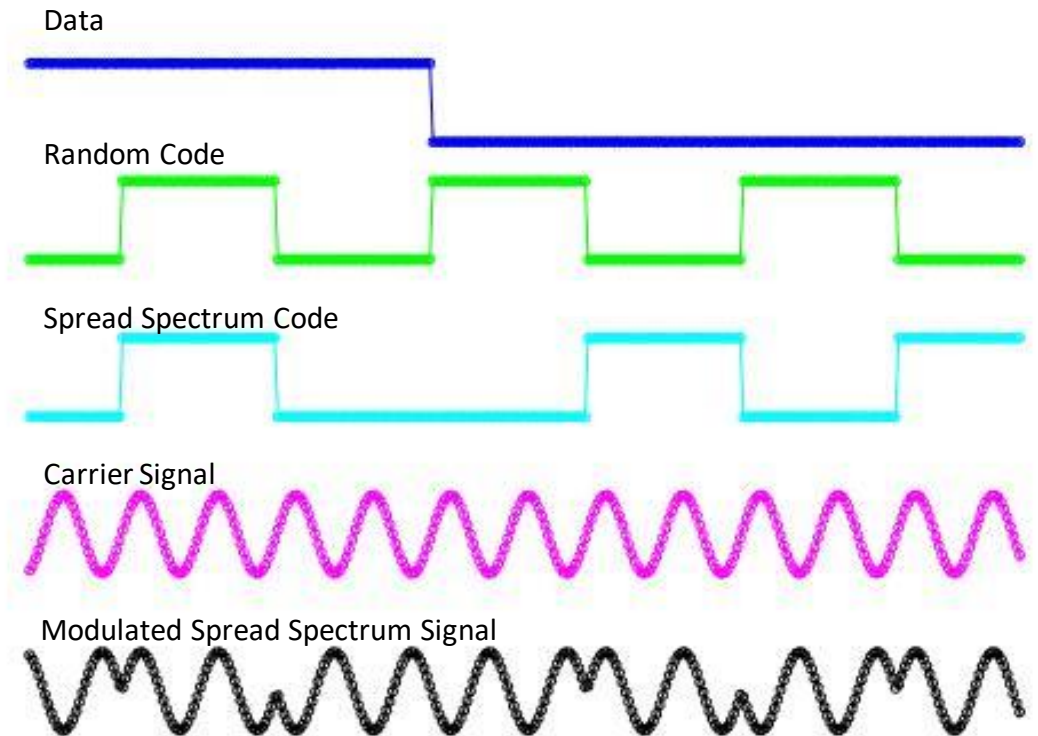
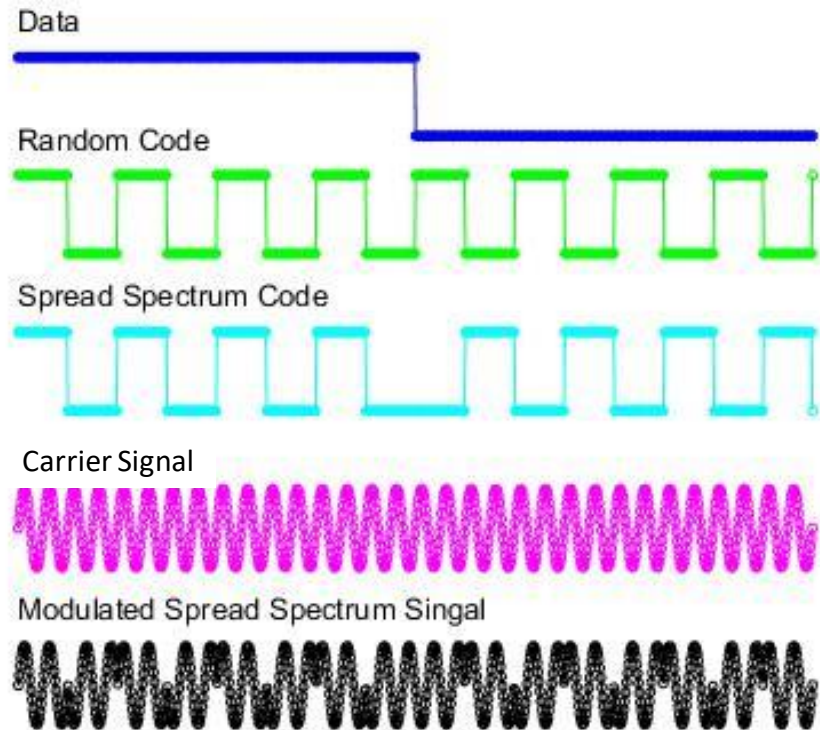
# Auto-Correlation and Cross-Correlation Properties of C/A Code





# Carrier, Code and Data Modulation Example

## BPSK (Binary Phase Shift Keying)



SS : Spread Spectrum  
 DSSS : Direct Sequence Spread Spectrum  
 BPSK : Binary Phase Shift Keying

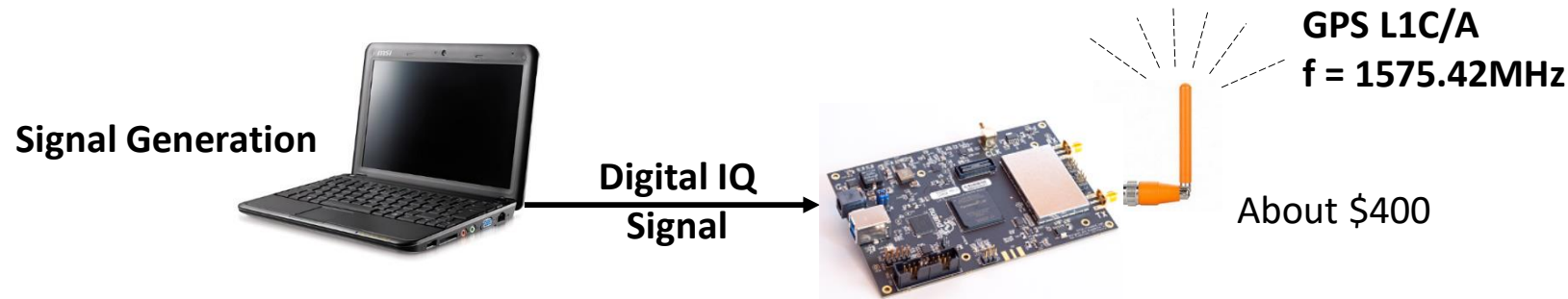
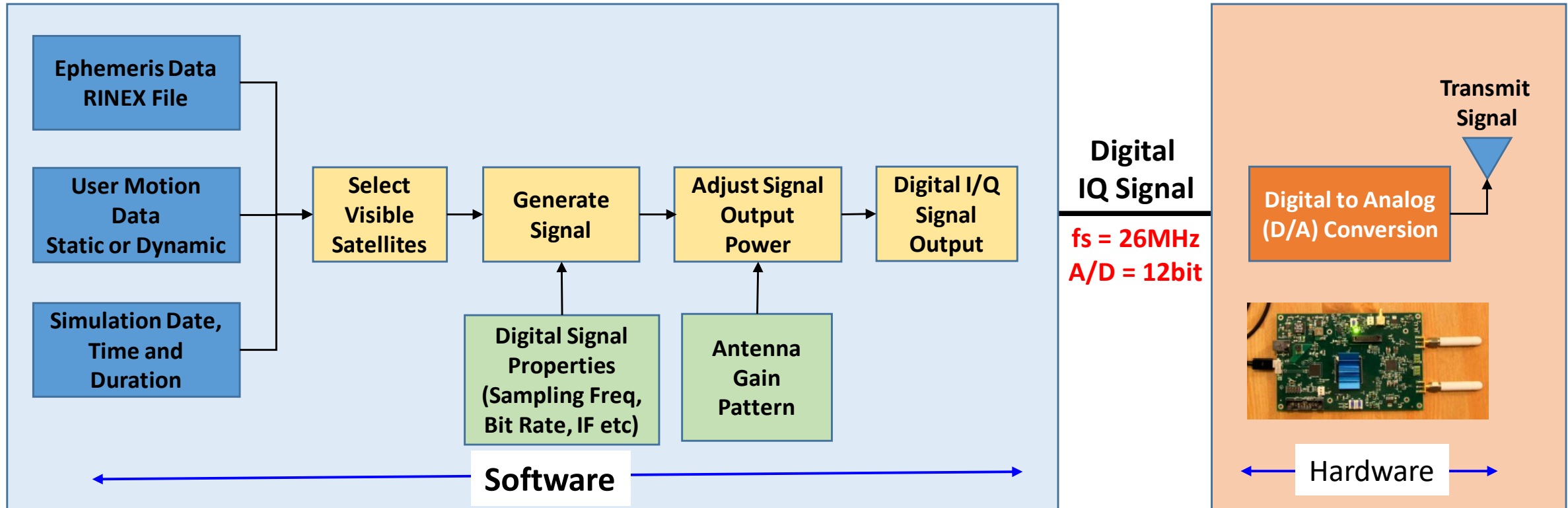
# Generate GPS L1C/A Signal

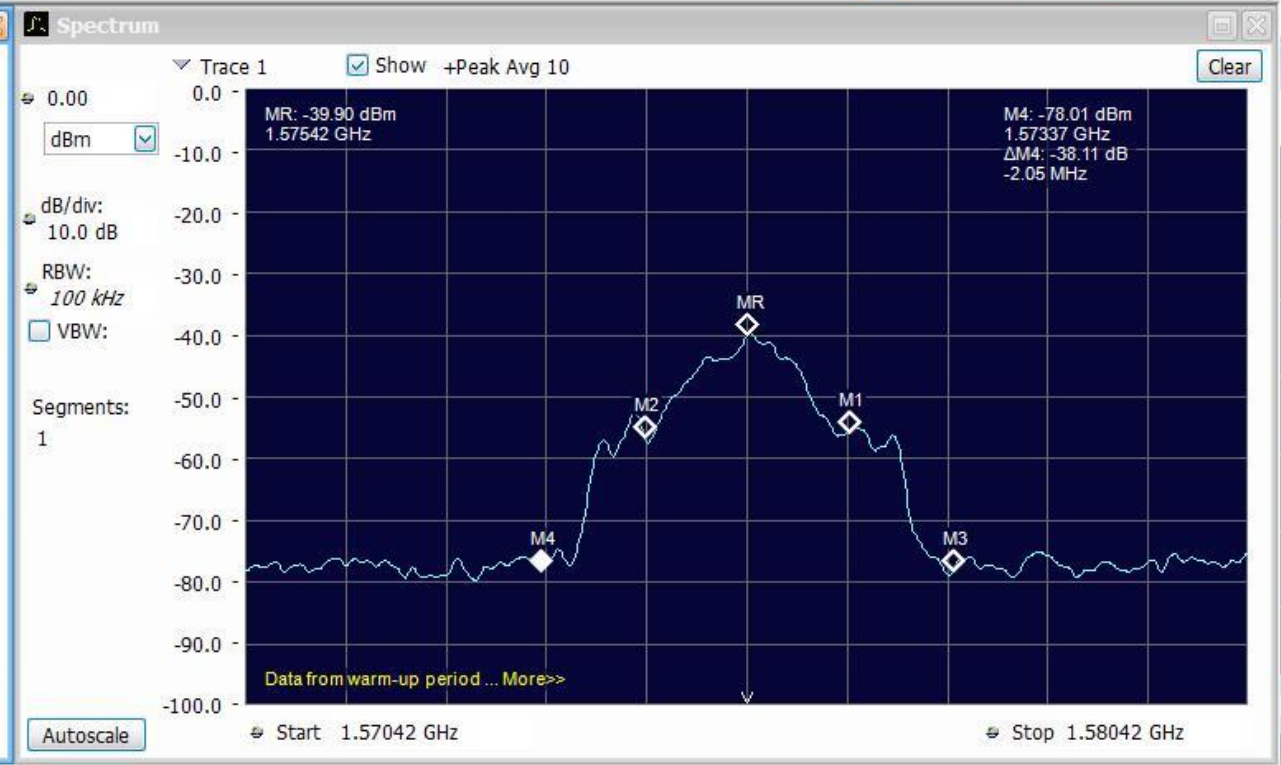
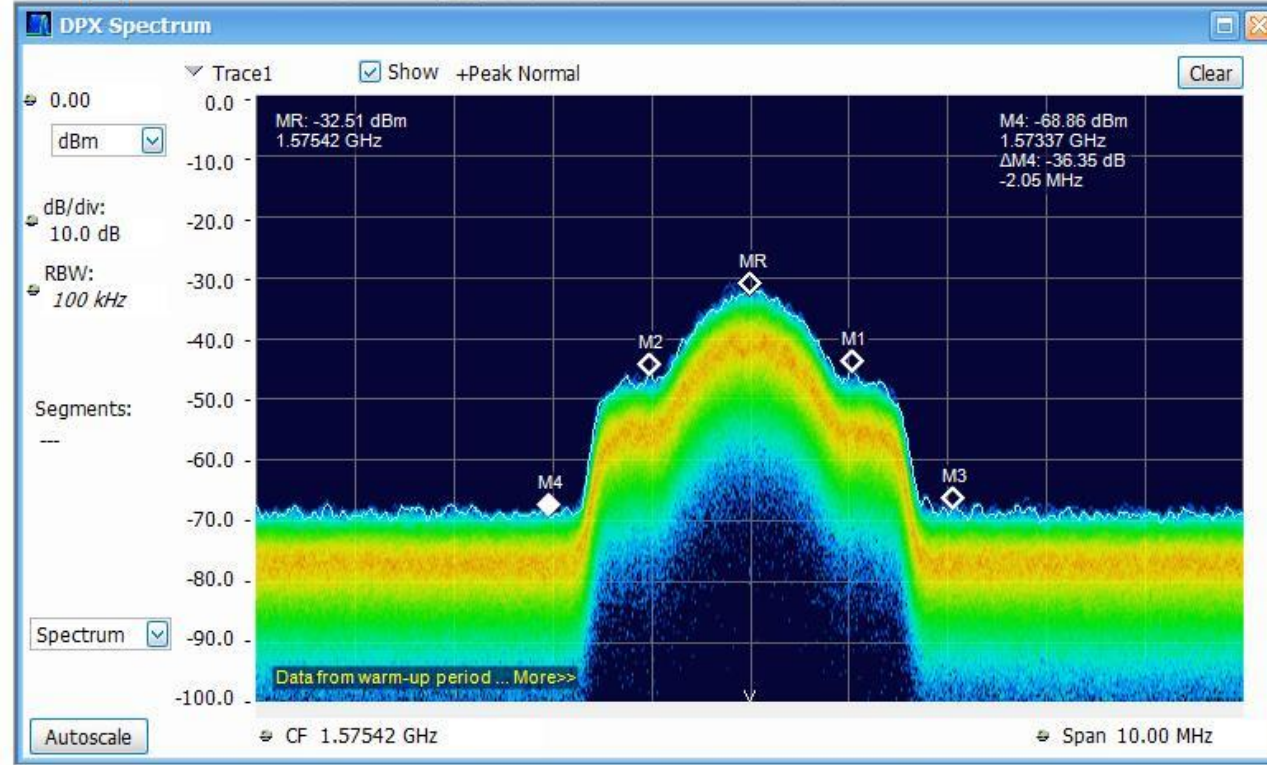
- Carrier Signal
  - Generate Carrier Signal
    - $C = A \cdot \cos(w \cdot t) = A \cdot \cos(2 \cdot \pi \cdot f_c \cdot t)$
    - $f_c$  = Carrier frequency or center frequency
    - $A$  = amplitude or signal power
- PRN Code
  - Generate as specified in the GPS IS Document
- Navigation Data
  - Generate as specified in the GPS IS Document
  - Data Rate : 50bps
  - 1 word : 30bits
  - 1 sub-frame : 300bits (6 sec)
    - 10 words / sub-frame
  - 1 frame : 1500bits (30 sec)
    - 5 sub-frames/frame

# Generate GPS L1C/A Signal

- Generate GPS L1C/A signal in computer
  - Digital IF signal
  - Signal is generated at IF level
    - For example:
      - IF (Intermediate Frequency) : 4MHz
      - Sampling Frequency : 16MHz
      - A/D Resolution : 4bit
- Convert the digital IF signal to analog RF signal
  - Use Software Radio Device
    - Up-convert from IF to RF
      - Generate RF signal at 1575.42MHz (analog signal)
      - Transmit the signal from antenna

# Low-Cost GPS Signal Generator





### DPX Settings

✕

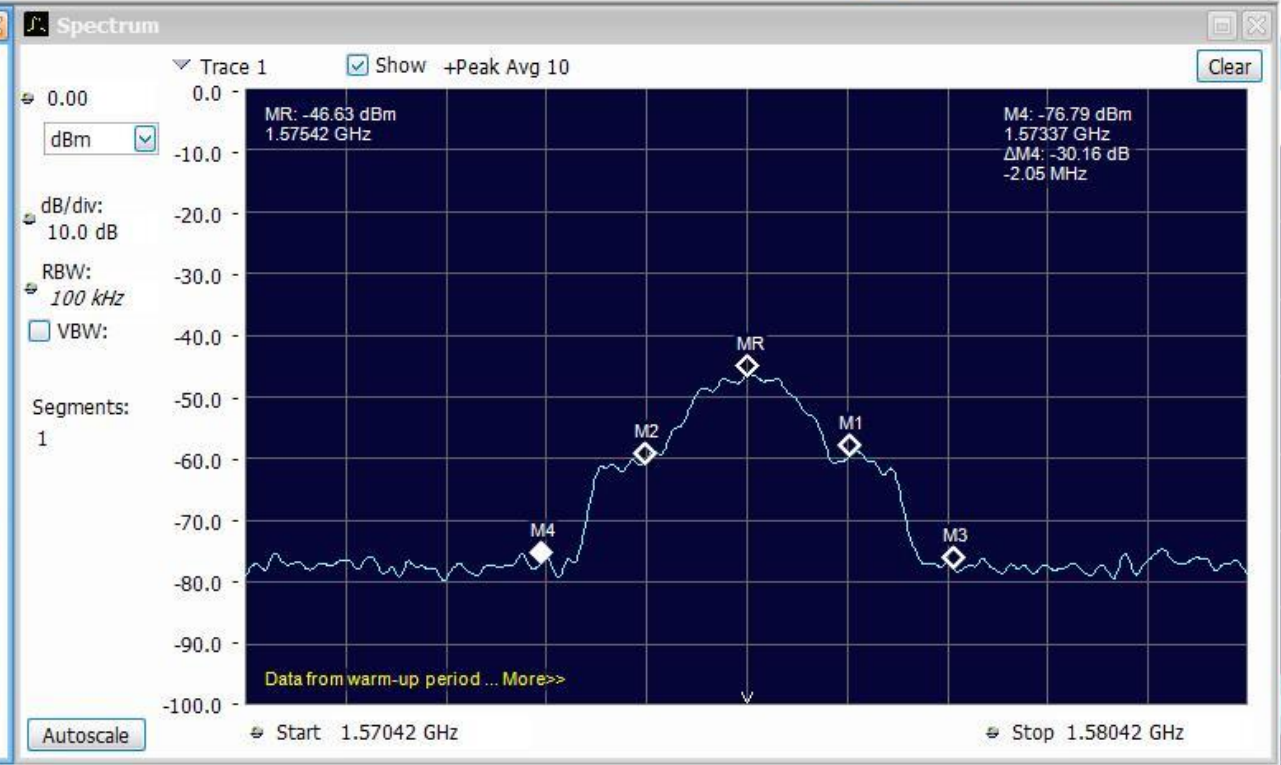
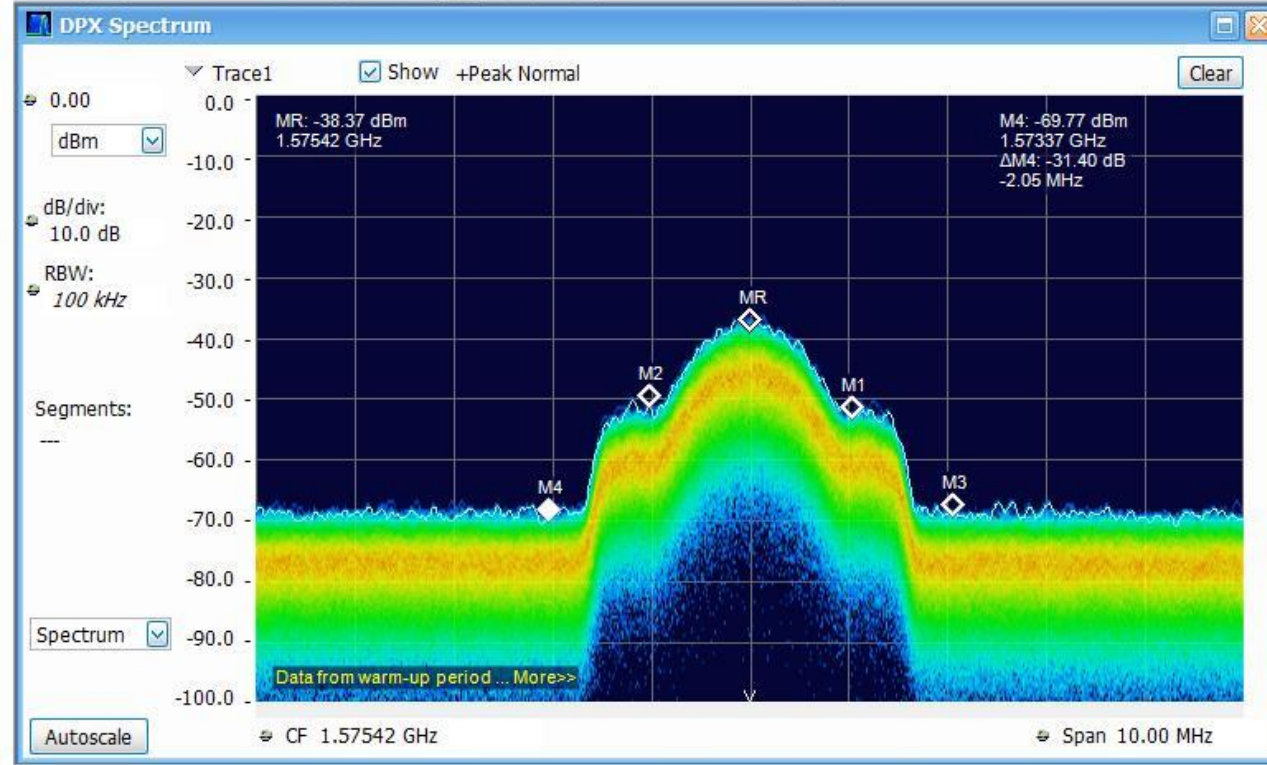
Frequency:  Span:

Start:  Step Size:   Auto

Stop:  Dwell time:   Auto (swept only)

Markers            ✕

DPX Spectrum Frequency  Ref Lev  Span  Res BW



### DPX Settings

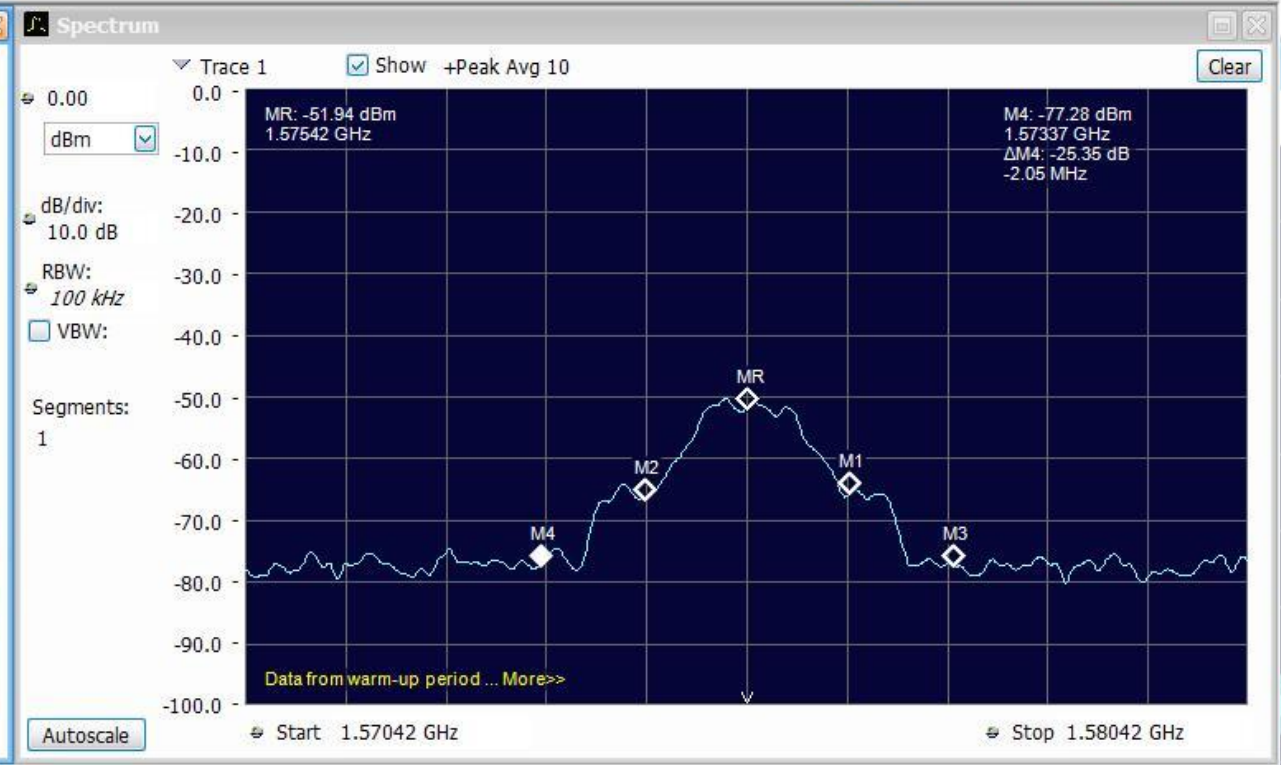
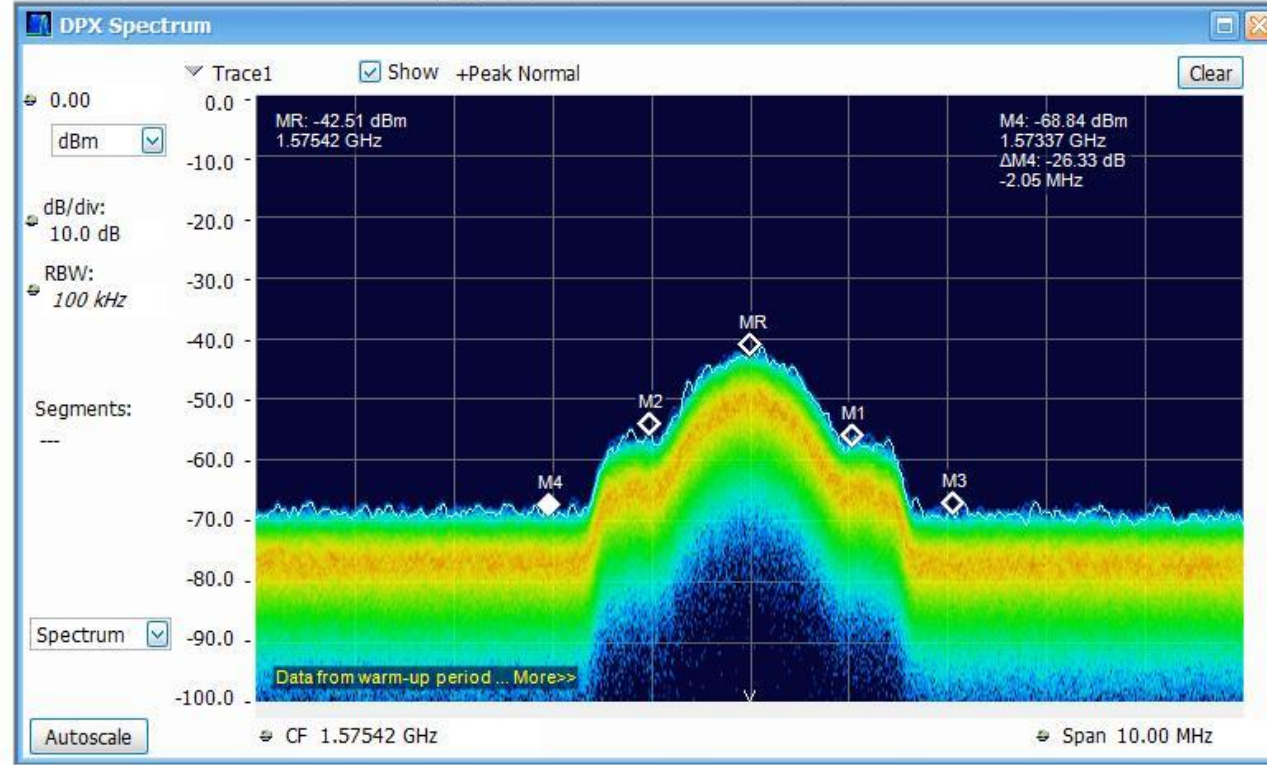
Frequency: 1.57542 GHz    Span: 10.00 MHz   

Start: 1.57042 GHz    Step Size: 1.0000 MHz     Auto

Stop: 1.58042 GHz    Dwell time: 50.0 ms     Auto

Markers ▼ M4       Frequency ▼ 2.05 MHz

DPX Spectrum Frequency 1.57542 GHz Ref Lev 0.00 dBm Span 10.00 MHz Res BW 100 kHz



### DPX Settings

✕

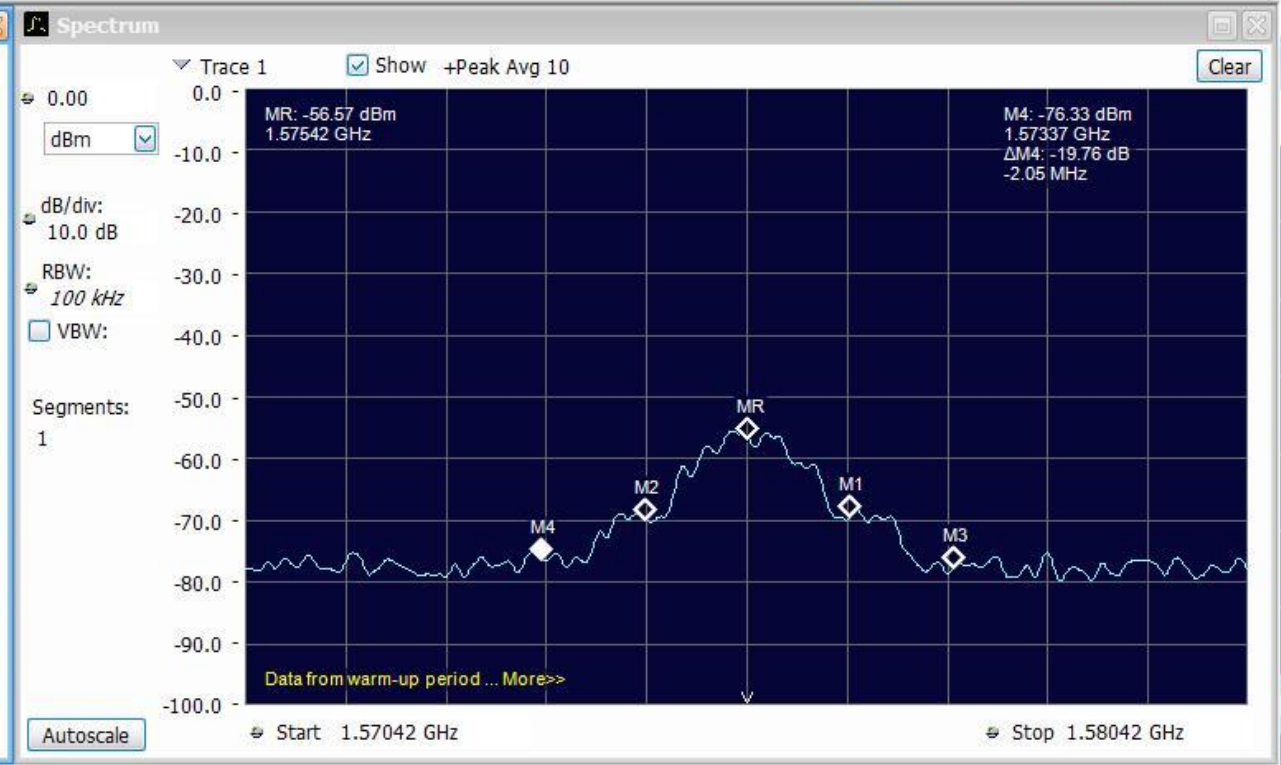
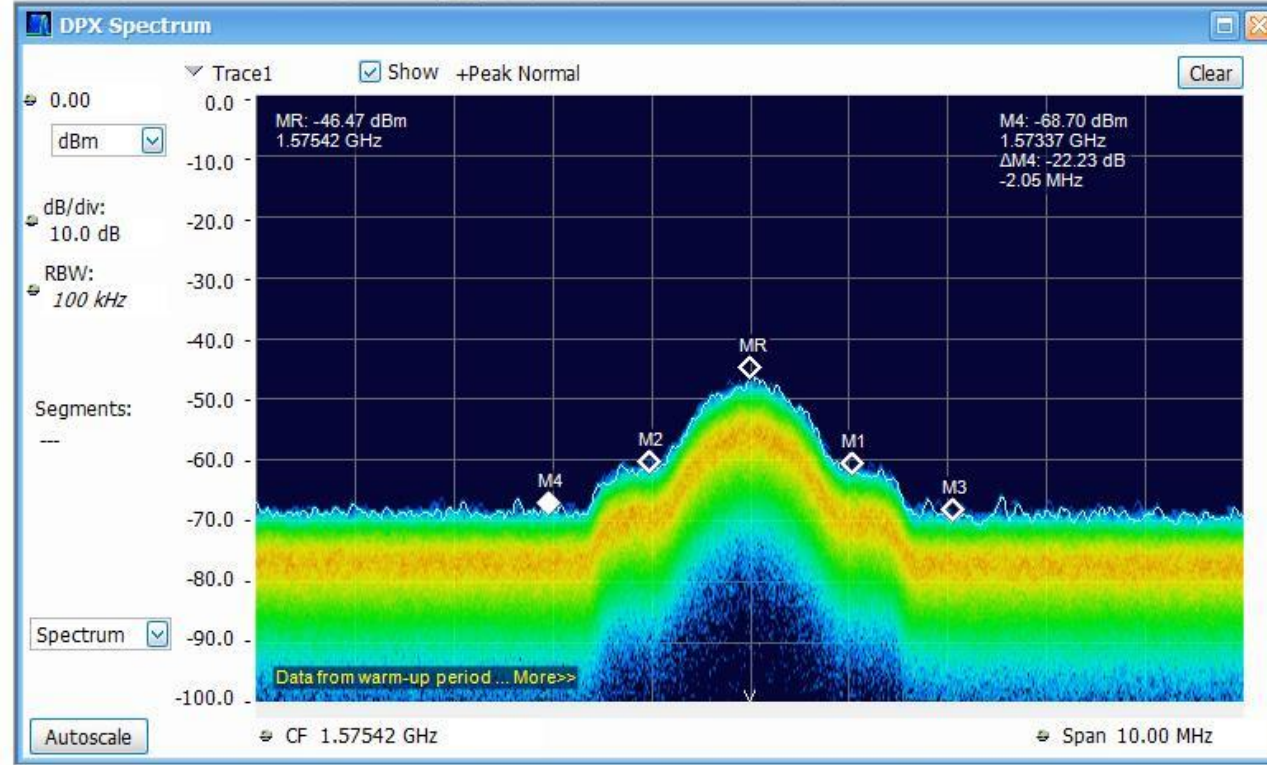
Frequency:  Span:

Start:  Step Size:   Auto

Stop:  Dwell time:   Auto (swept only)

Markers            ✕

DPX Spectrum Frequency  Ref Lev  Span  Res BW



### DPX Settings

✕

Frequency:  Span:

Start:  Step Size:   Auto

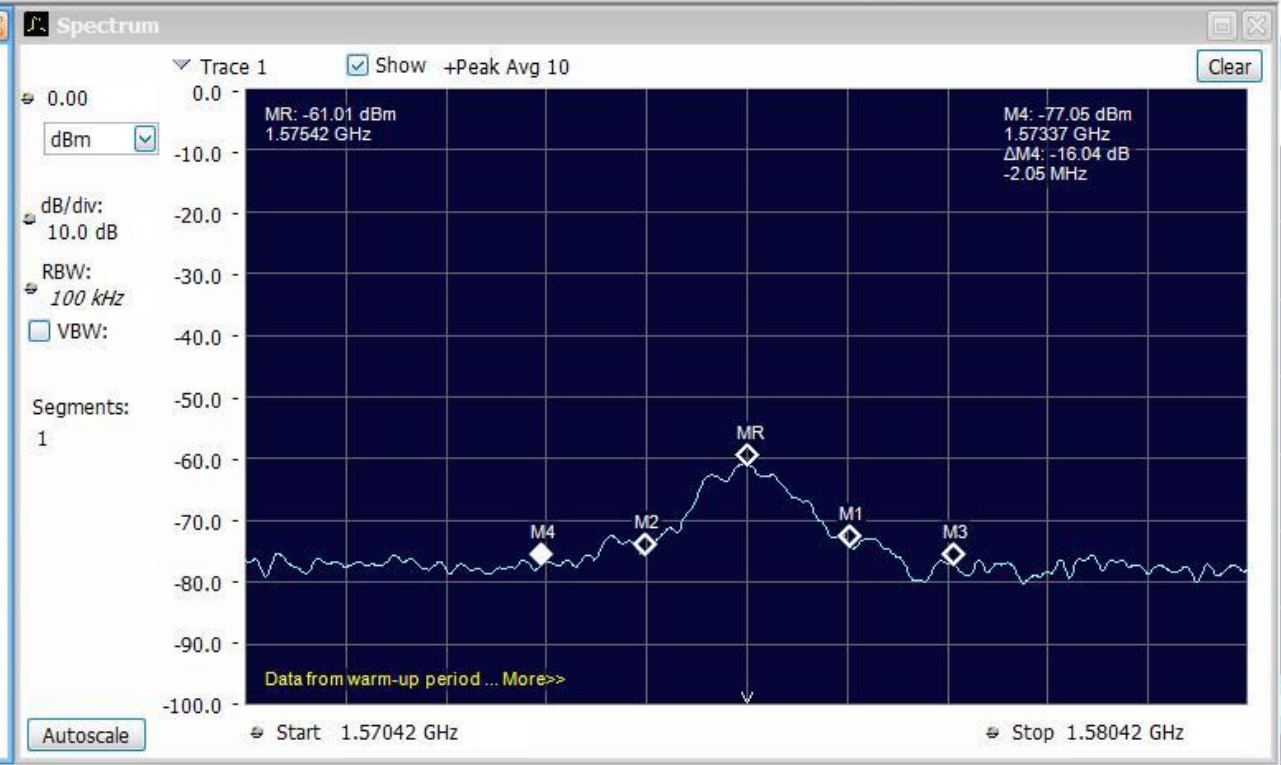
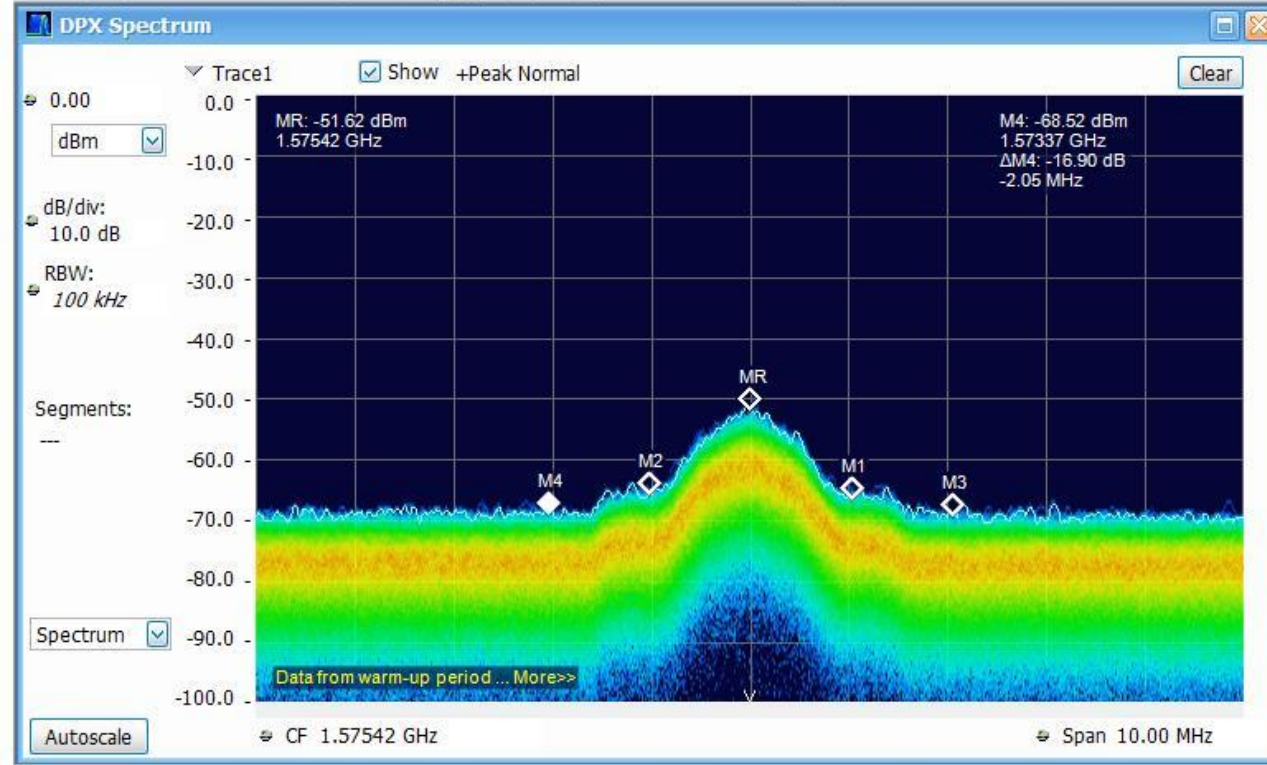
Stop:  Dwell time:   Auto (swept only)

Markers

DPX Spectrum Frequency  Ref Lev  Span  Res BW

Analyzing Warm-up period Real Time Free Run Ref: Int 24





### DPX Settings

Freq & Span | BW | Traces | Horiz & Vert Scale | Bitmap Scale | Prefs | Density

Frequency: 1.57542 GHz Span: 10.00 MHz Max Span

Start: 1.57042 GHz Step Size: 1.0000 MHz  Auto

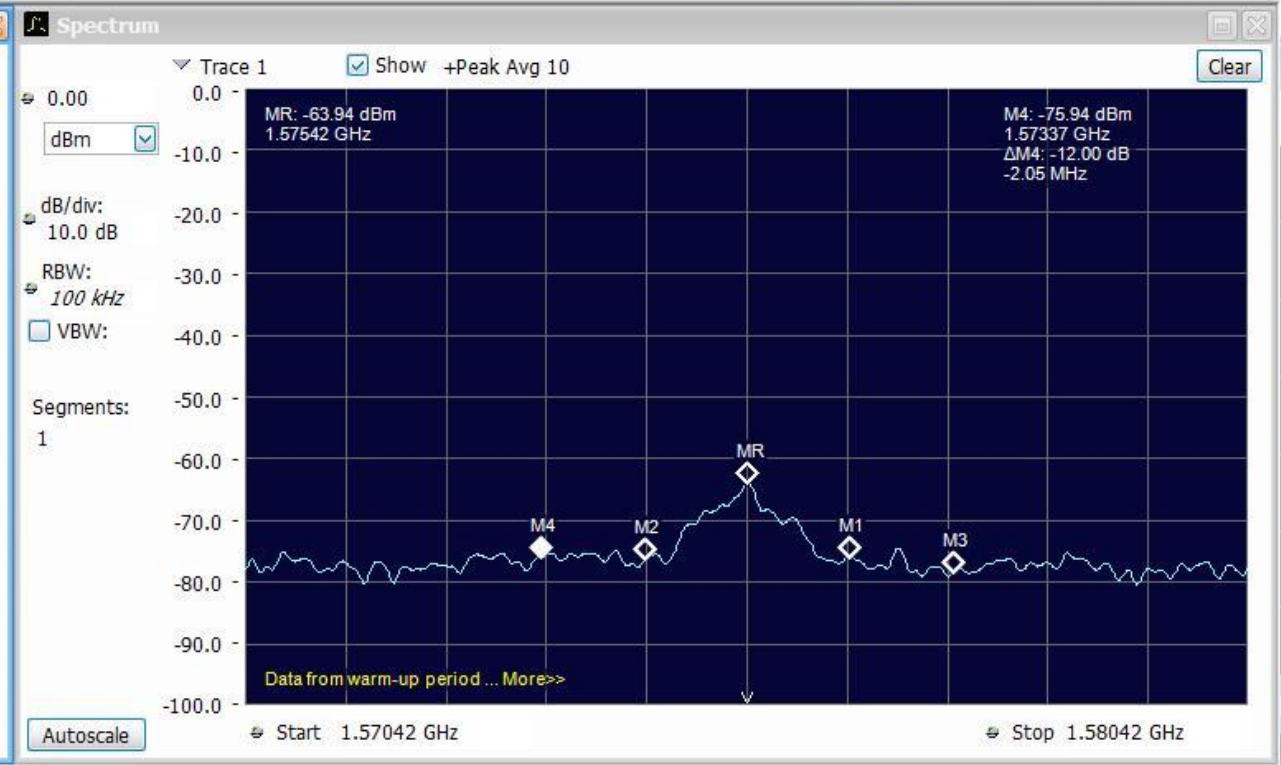
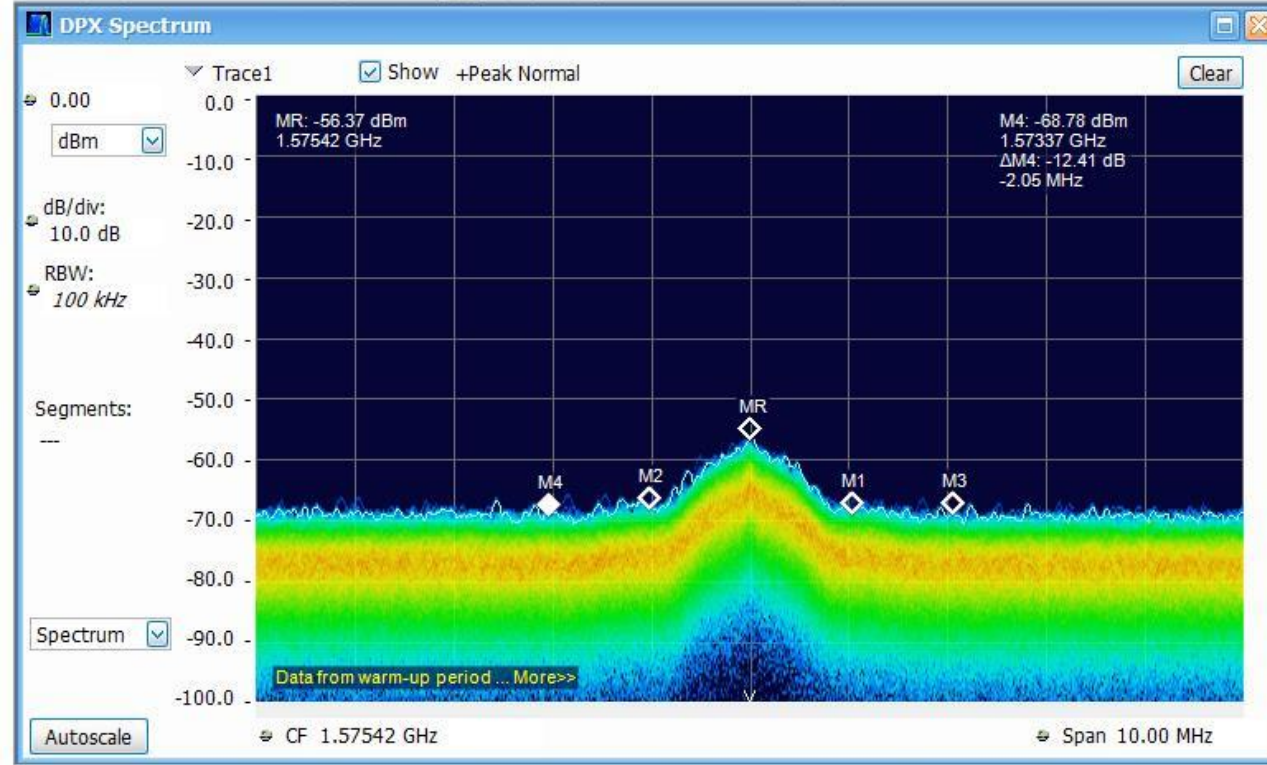
Stop: 1.58042 GHz Dwell time: 50.0 ms  Auto

(swept only)

Restore Defaults X

Markers ▼ M4 To Center Peak ← → ↓ ↑ Frequency ▼ 2.05 MHz Table Define X

DPX Spectrum Frequency 1.57542 GHz Ref Lev 0.00 dBm Span 10.00 MHz Res BW 100 kHz Markers Traces ⚙



### DPX Settings

✕

Frequency:  Span:

Start:  Step Size:   Auto

Stop:  Dwell time:   Auto (swept only)

Markers ▼ M4 To Center Peak ← → ↓ ↑

Frequency ▼  Table Define ✕

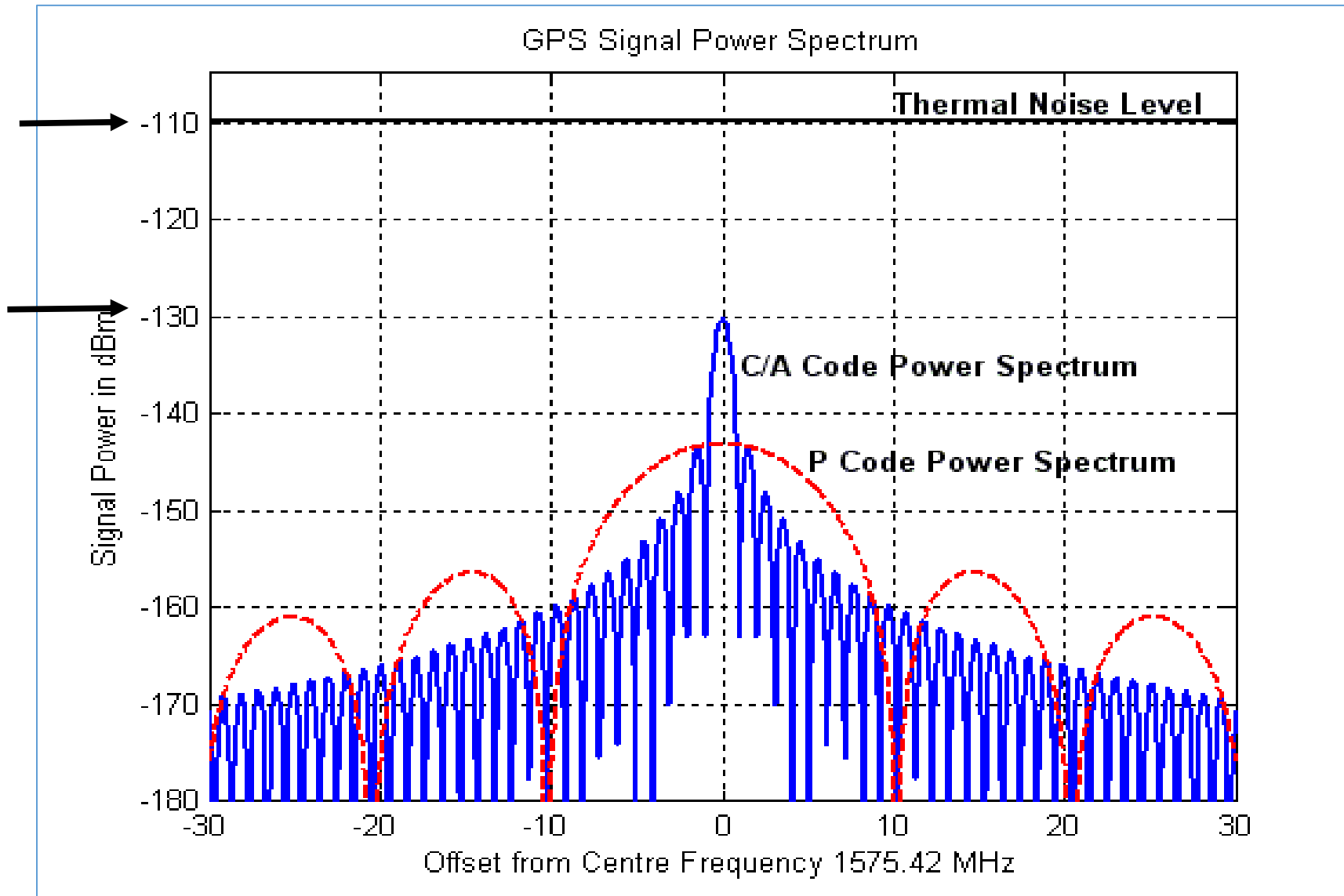
DPX Spectrum Frequency  Ref Lev  Span  Res BW  Markers Traces ⚙

# GPS Signal Power

Noise Power  
Any Signal below this  
noise level can't be  
measured in a  
Spectrum Analyzer

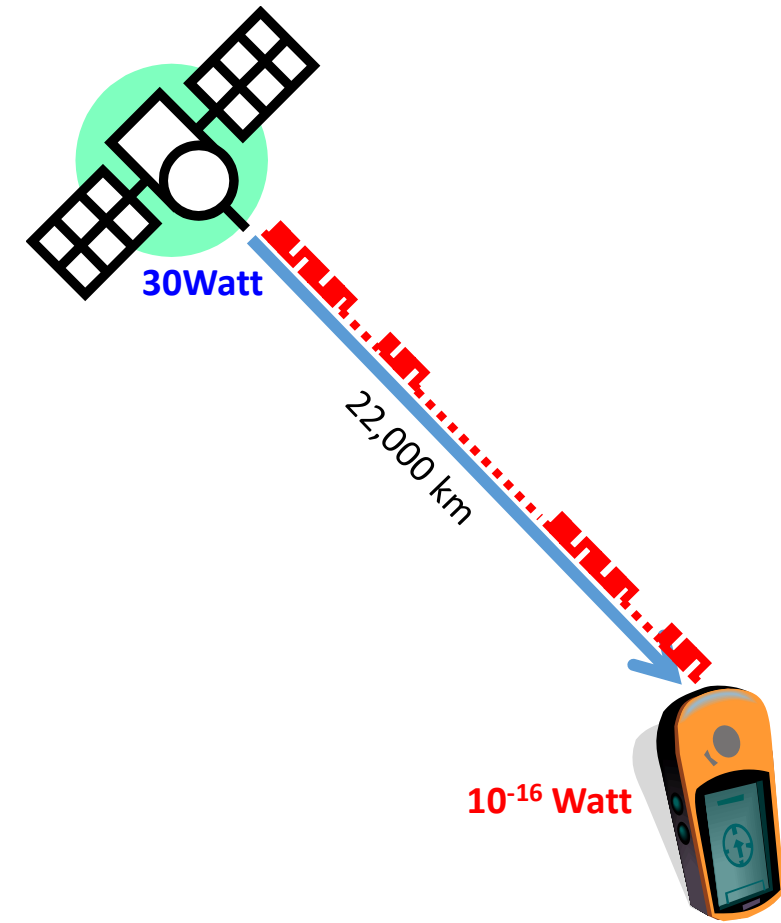
GPS Signal Power at  
Antenna, -130dBm

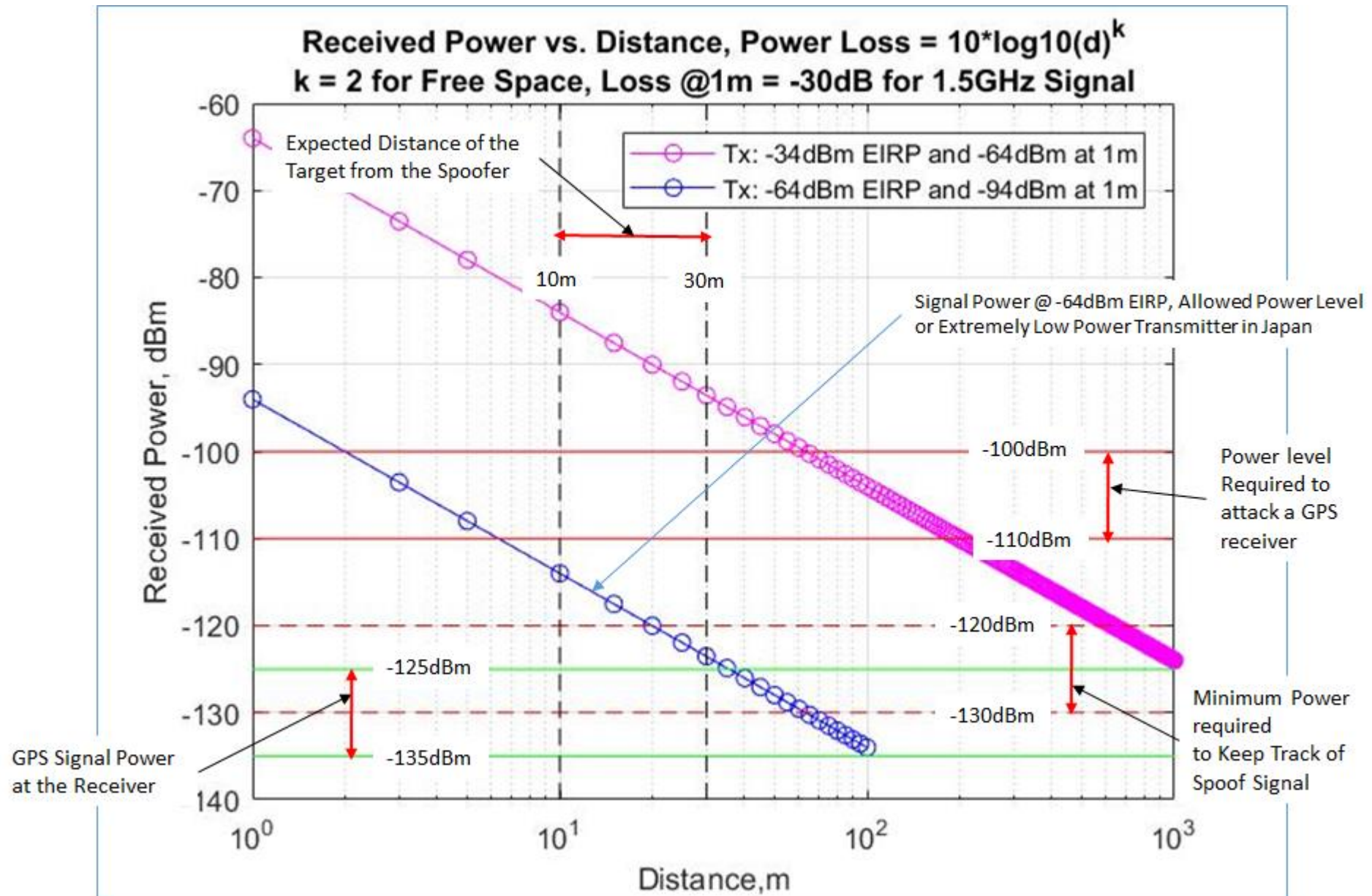
Mobile phone, WiFi,  
BT etc have power  
level above -110dBm,  
much higher than GPS  
Signal Power

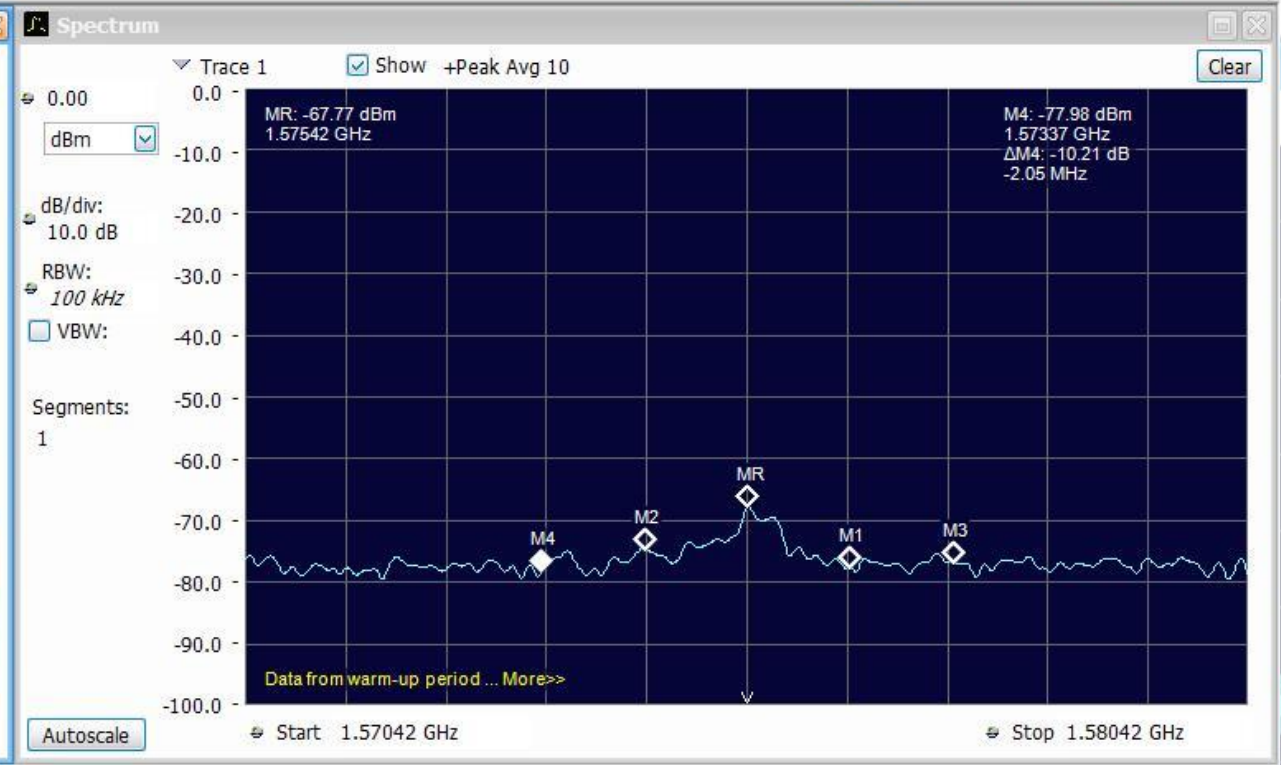
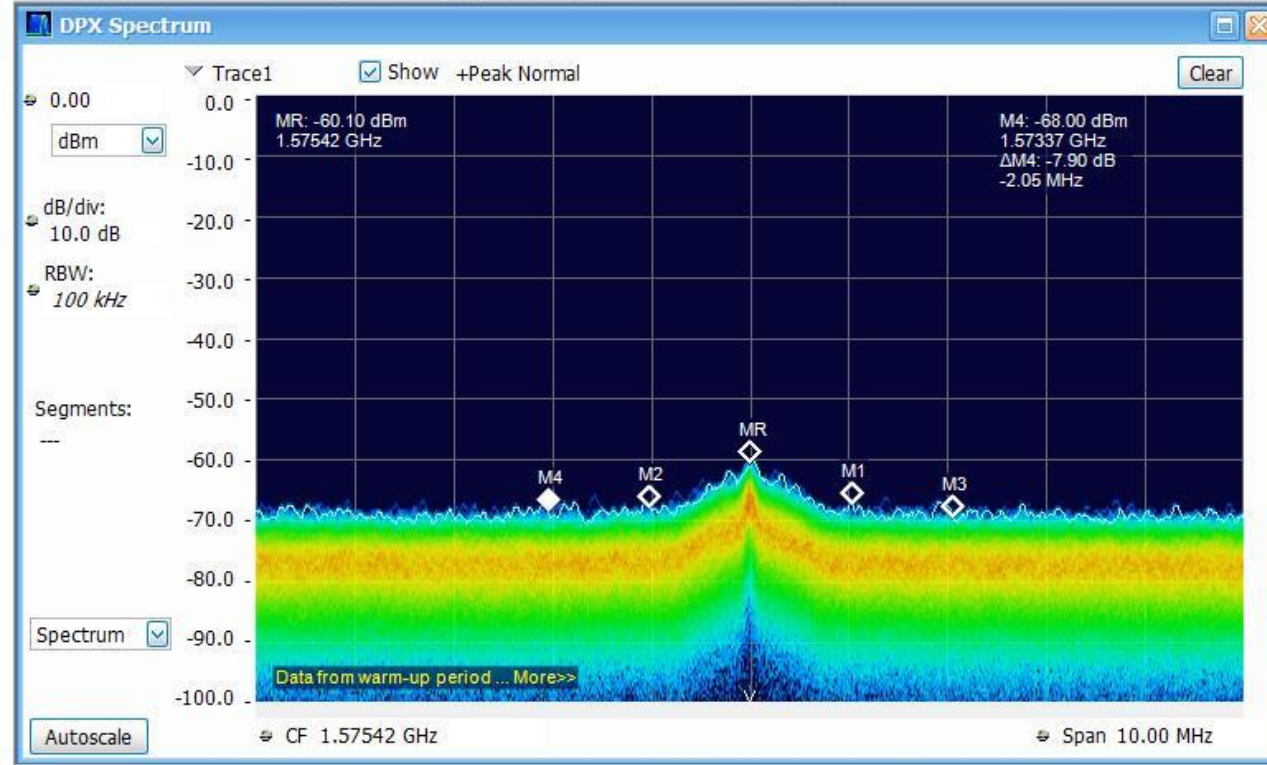


# GPS Signal Power, How Strong or How Weak?

- GPS satellites are about 22,000km away
- Transmit power is about 30W
- This power when received at the receiver is reduced by  $10^{16}$  times.
  - The power reduces by  $1/\text{distance}^2$
  - This is similar to seeing a 30W bulb 22,000Km far
- GPS signals in the receiver is about  $10^{-16}$  Watt, which is below the thermal noise







### DPX Settings

✕

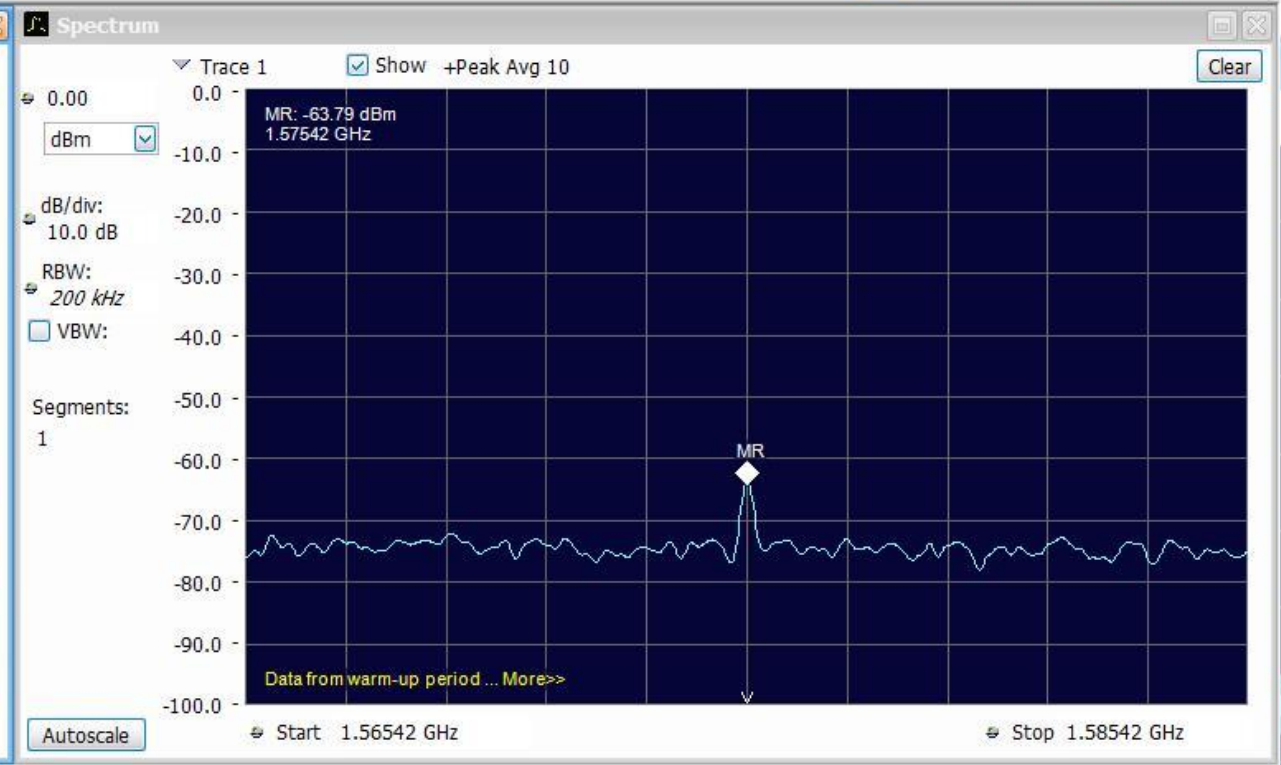
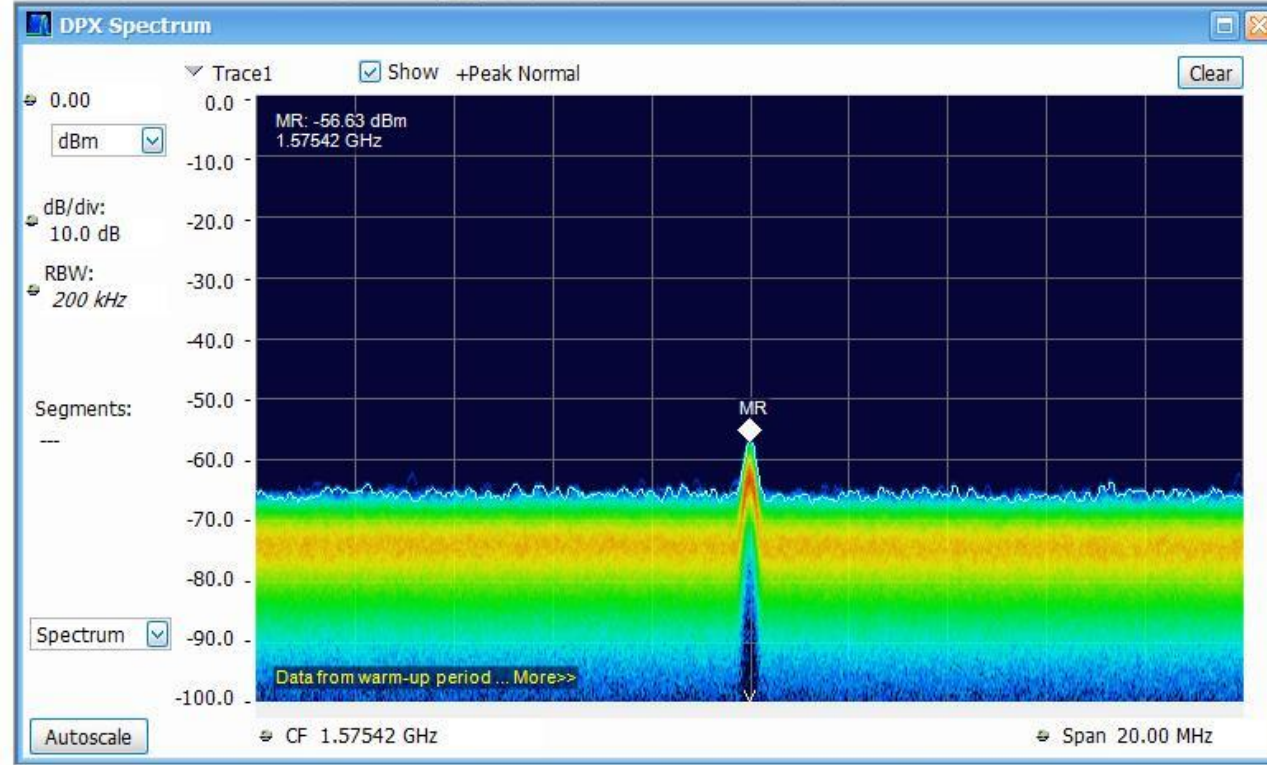
Frequency:  Span:

Start:  Step Size:   Auto

Stop:  Dwell time:   Auto (swept only)

Markers            ✕

DPX Spectrum Frequency  Ref Lev  Span  Res BW



### DPX Settings

Frequency: 
 Span:

Start: 
 Step Size: 
 Auto

Stop: 
 Dwell time: 
 Auto

Markers MR       Frequency

DPX Spectrum Frequency  Ref Lev  Span  Res BW

# SNR & C/No

- SNR
  - Signal to Noise Ratio, unit is dB
  - S: Signal Power in dBm or dBW
  - N: Noise power in a given bandwidth in dBm or dBW
- C/No
  - Carrier to Noise Density, unit is dB-Hz
  - C: Carrier power in dBm or dBW
  - No: Noise power density in dBm-Hz or dBW-Hz
- $SNR = C/No - BW$  (BW = bandwidth of the Front End)
  - If  $BW = 4\text{Mhz} = 10 \cdot \log_{10}(4000000) = 66\text{dB}$
  - If  $C/No = 48\text{dB-Hz}$
  - $SNR = C/No - BW = 45 - 66 = -21\text{dB}$
- C/No from Received Signal Power
  - Noise Density (No) at Room Temperature (290K):  $-204\text{dBW/Hz}$
  - Received Power (GPS L1C/A Signal) at Antenna:  $-158.5\text{dBW}$  or  $-128.5\text{dBm}$
  - $C/No = -158.5 - (-204) = 45.5\text{dB-Hz}$



# Contact Information

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Associate Professor(Project)

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